

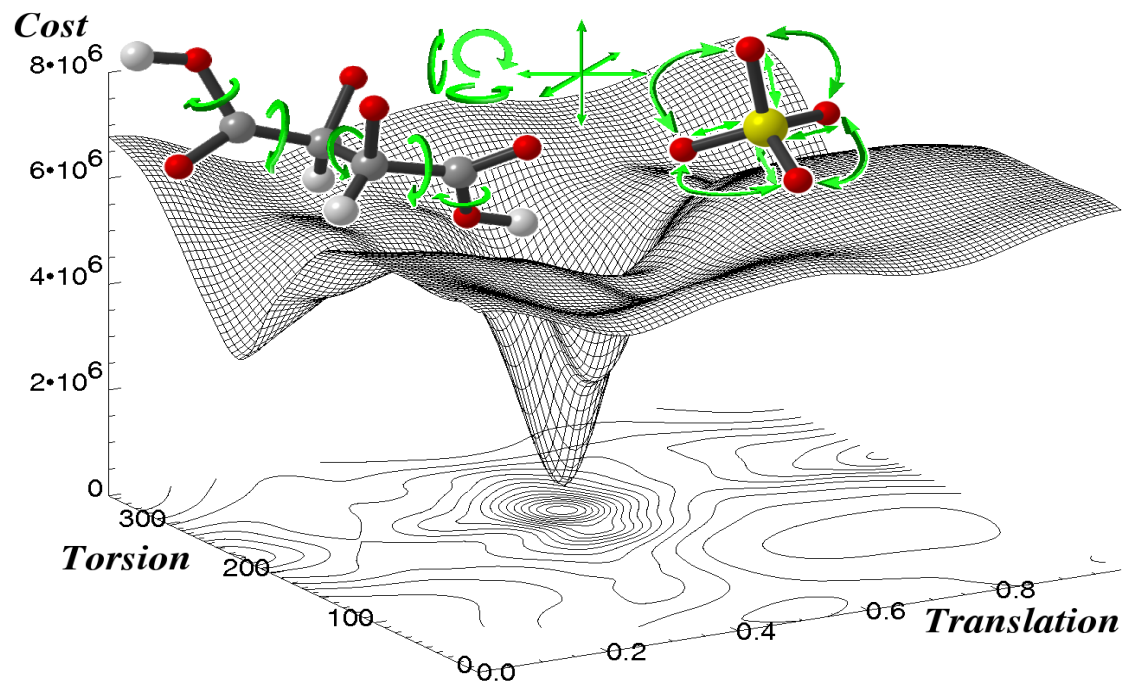


## ***Structure solution in direct space using Fox and smart restraints***

***Vincent Favre-Nicolin***

*CEA, INAC, SP2M & Université Joseph Fourier – Grenoble, France*

<http://vincefn.net/reciprocs/>



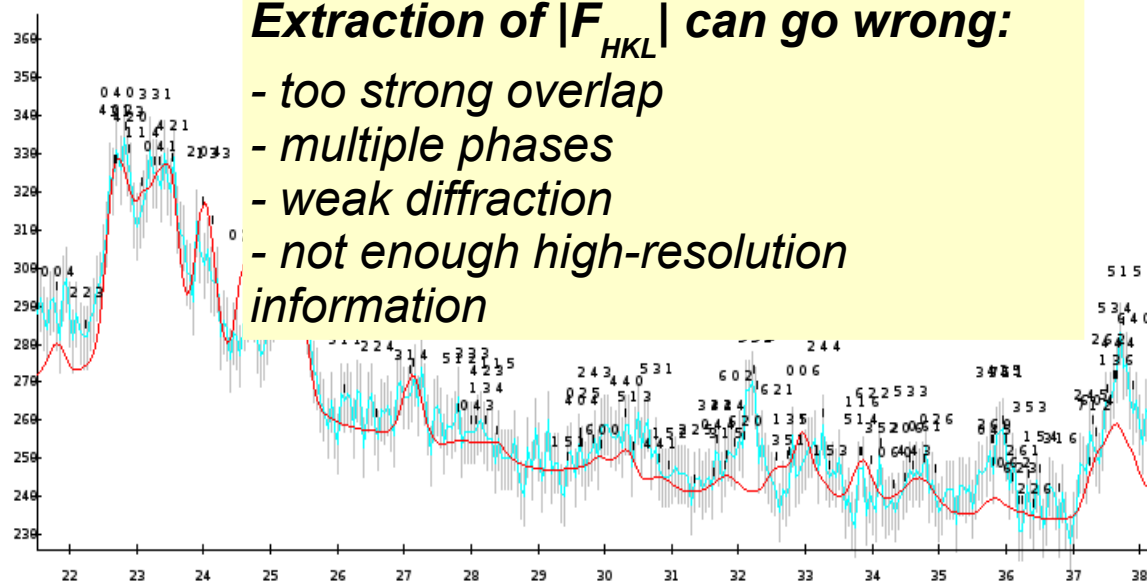
# ***Introduction: Structure Determination in Direct Space***

# Real (Direct)-Space Methods vs. Reciprocal-Space (Direct) Methods

## Powder diffraction :

Extraction of  $|F_{HKL}|$  can go wrong:

- too strong overlap
- multiple phases
- weak diffraction
- not enough high-resolution information



## Single Crystal:

- twinning/reflexion overlap
- no high resolution data available

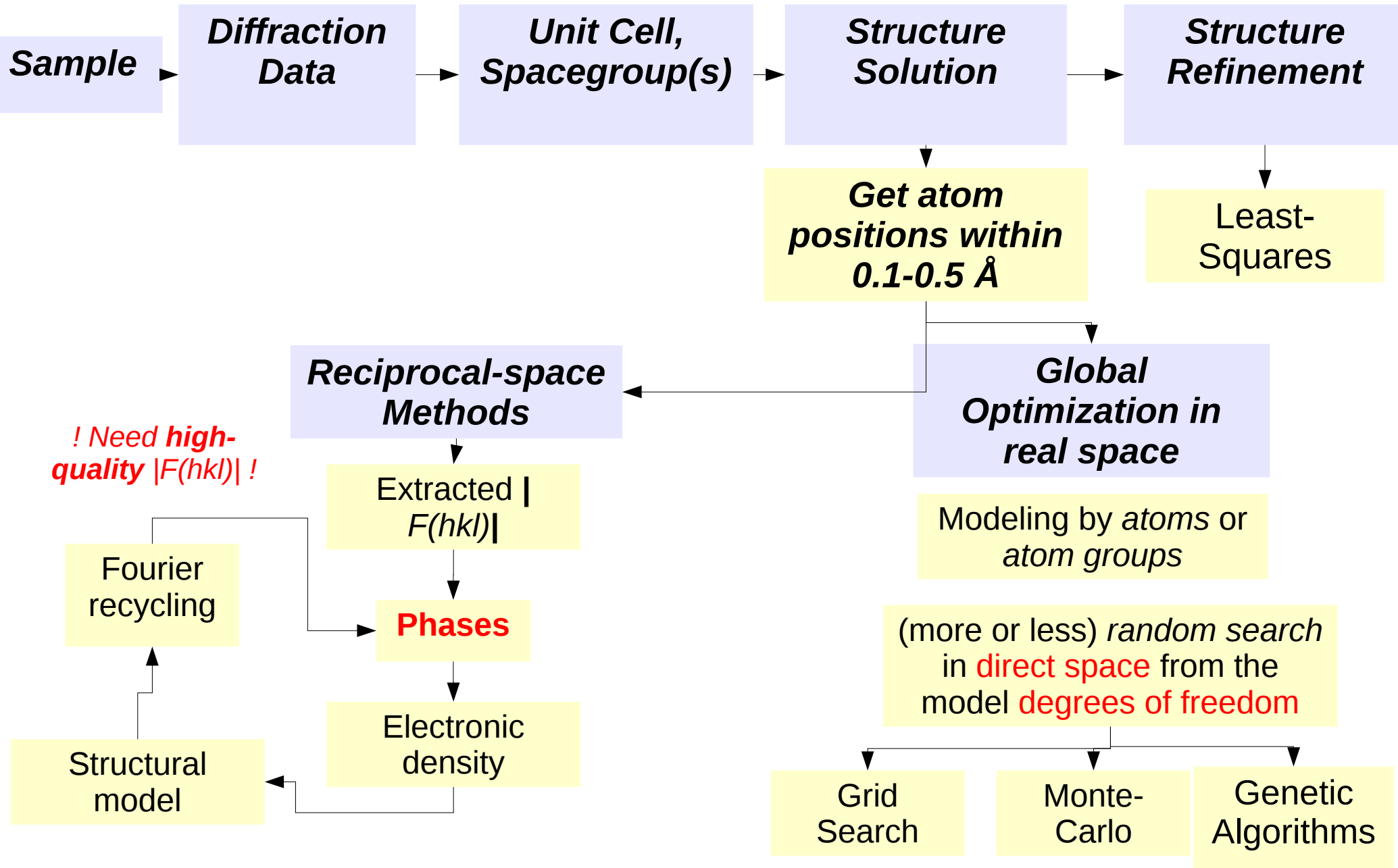
Direct methods are powerful (using full crystallographic formalism to derive the electronic density in seconds) but may not recover from bad structure factors

Real-Space structure solution: try **many** configurations until a satisfactory one is found  
=> **brute-force approach** enabled by the increase in computing power  
A **basic but robust** approach to structure solution

### Limited requirements on data resolution :

need more observed  $|F_{hkl}|$  than parameters (preferably many more)  
usually, a resolution of 2.5 Å is enough for most small molecules/inorganic structures,  
less if rigid bodies are used

# Solving Structures



# *Specifics of Fox*

## *Parametrization*

- **inorganic** or **organic** materials
- description using atoms, polyhedra, molecules
- automatic, smooth correction of **special positions**

## *Data*

- powder pattern (X-Ray, neutron, multi-phase, TOF, electron)
- single crystal
- **joint optimization** with several data sets
- use **integrated profiles** (no need to extract  $F(hkl)$ )

## *Algorithms*

- **Parallel Tempering** (Simulated Annealing)
- yields **multiple solutions**
- expandable to new algorithms

## *Other uses*

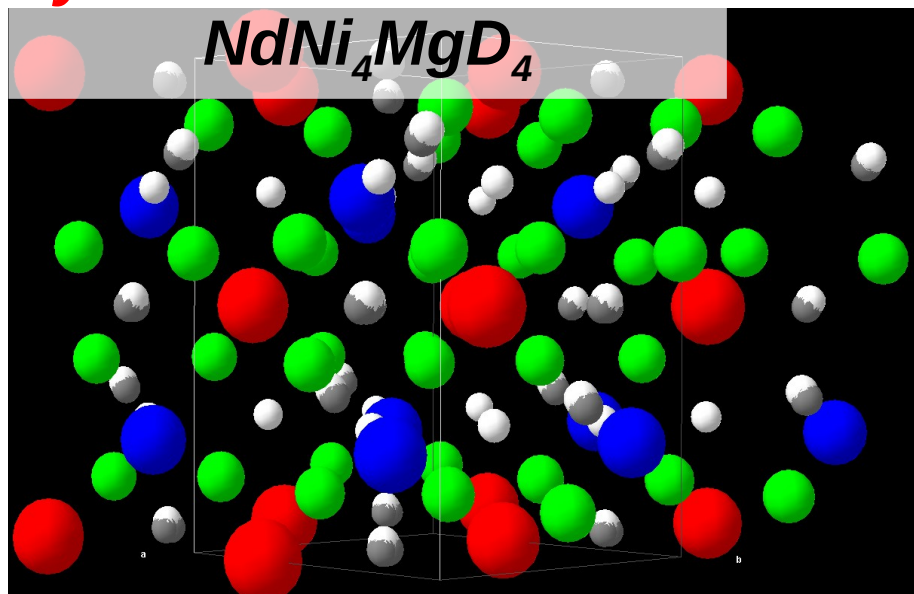
- display **Fourier maps** (from g<sub>gas</sub>/expgui or internally)
- **simulation** of powder & single crystal diffraction
- display data (crystal, powder) from **CIF file**

## *Availability*

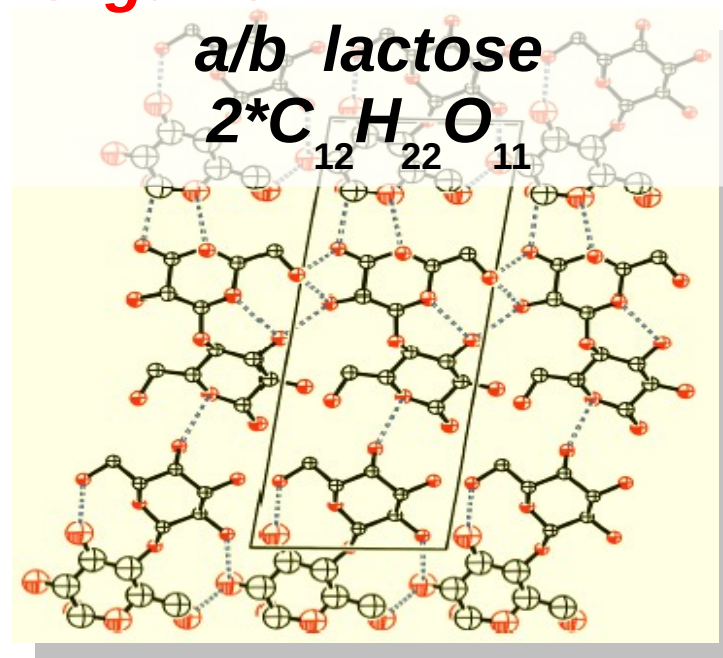
- **free** (<http://objcryst.sourceforge.net>)
- **open source** (GPL)
- available for *Linux*, *MacOS X* and *windows*

# Examples of structures solved

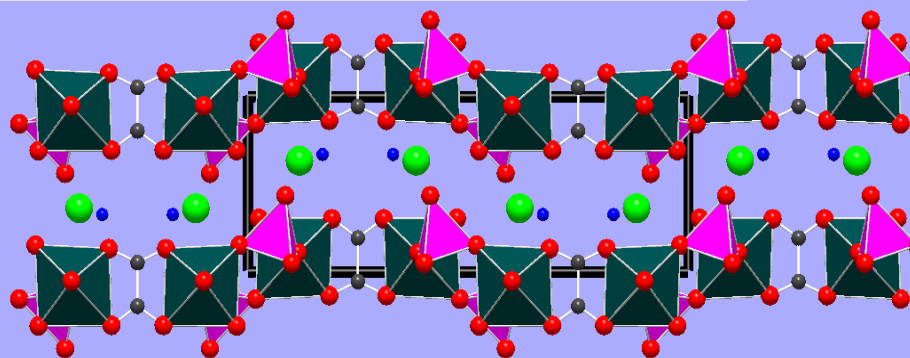
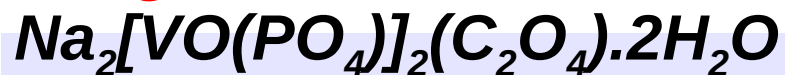
## Hydrides:



## Organic



## Inorganic:



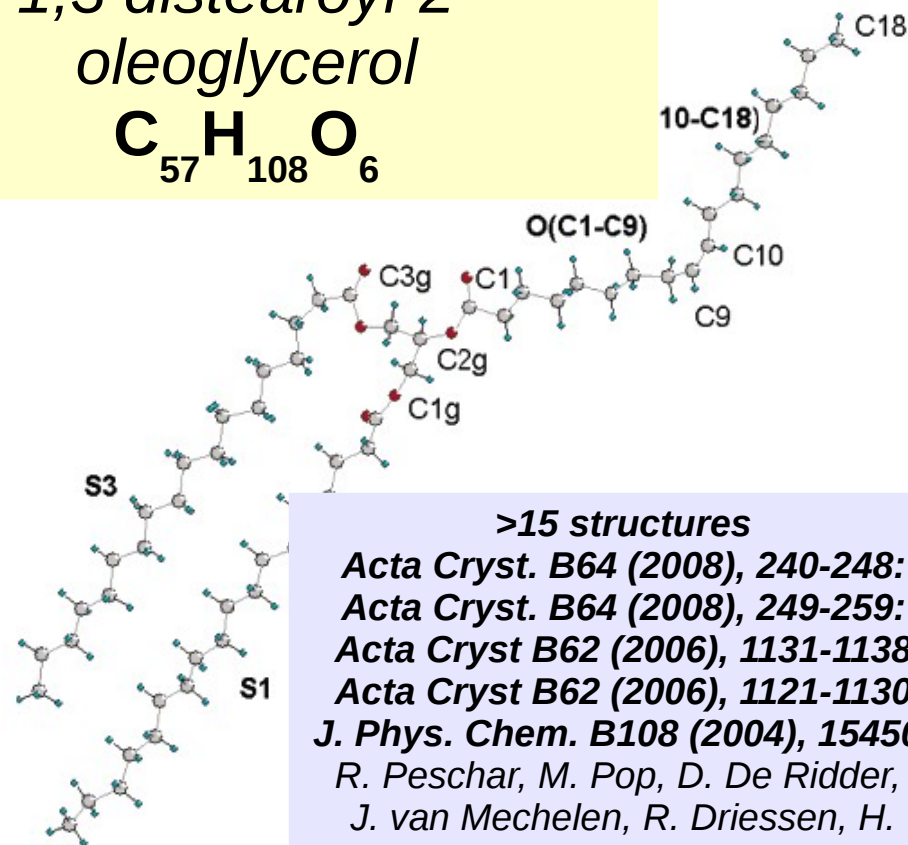
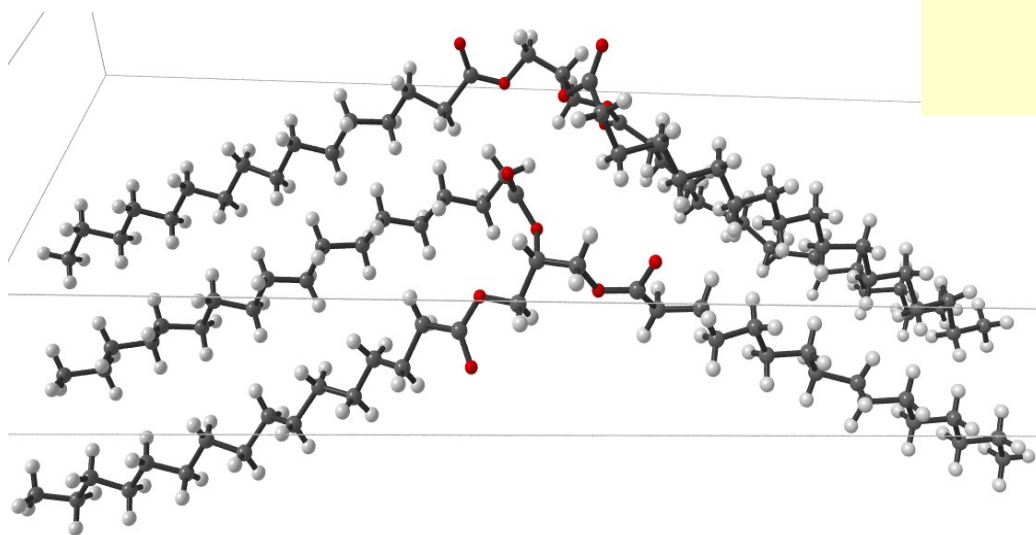
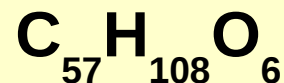
<http://objcryst.sourceforge.net/Fox/FoxBiblioStructures>

nce <http://vincefn.net/reciprocs/>

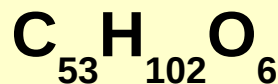


# Triglycerides

1,3 distearoyl-2-  
oleoglycerol



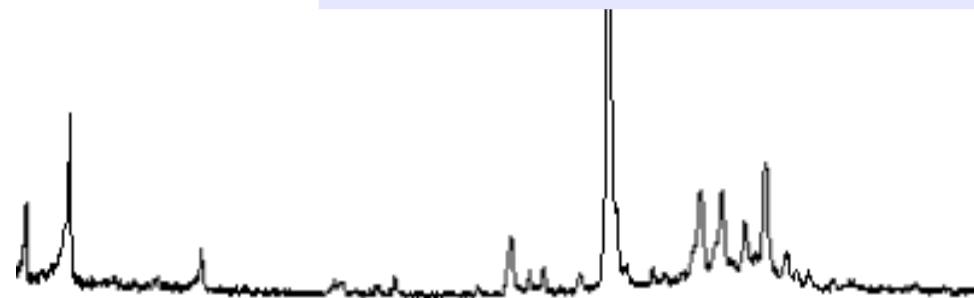
$\beta'$  PSP (1,3-di-*n*-hexadecanoyl-  
2-*n*-octadecanoyl glycerol)



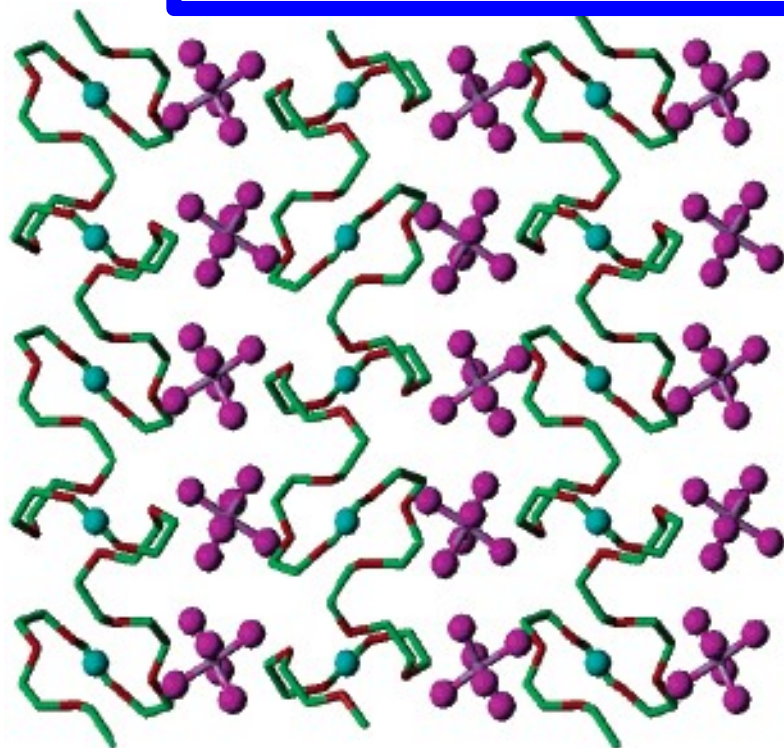
up to 56 non-H free torsion  
angles !

FOX > 2 months

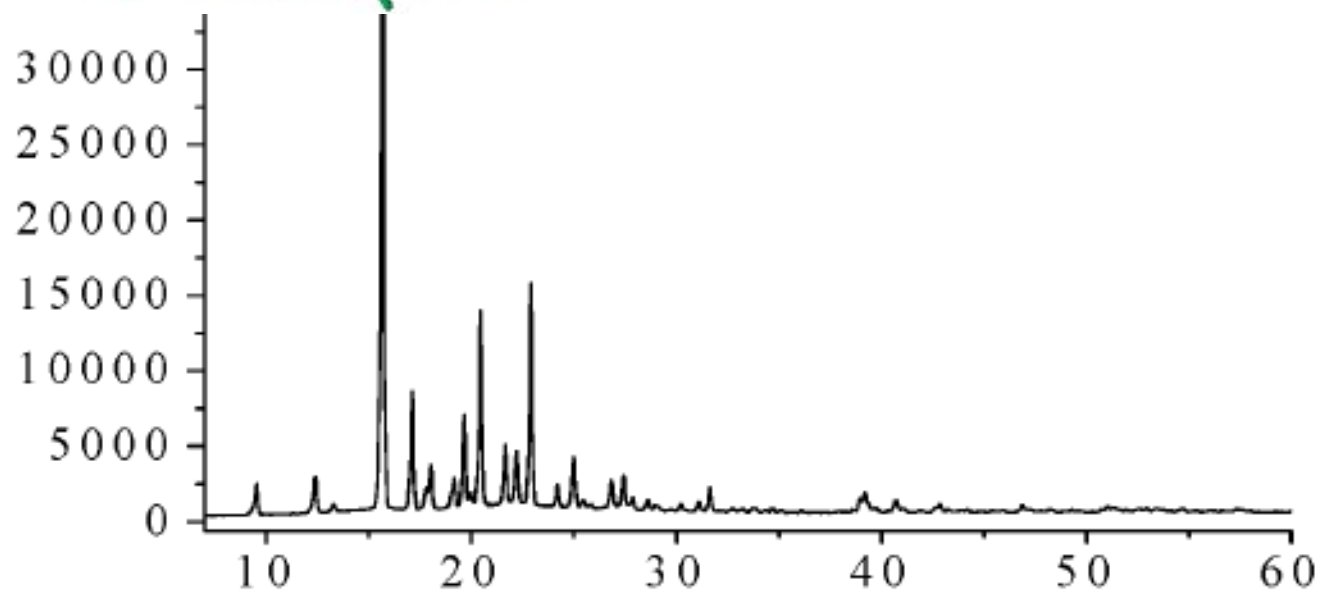
>15 structures  
*Acta Cryst. B64 (2008), 240-248:*  
*Acta Cryst. B64 (2008), 249-259:*  
*Acta Cryst B62 (2006), 1131-1138*  
*Acta Cryst B62 (2006), 1121-1130*  
*J. Phys. Chem. B108 (2004), 15450*  
R. Peschar, M. Pop, D. De Ridder,  
J. van Mechelen, R. Driessen, H.  
Schenk  
FOX + ORGANA



# Polymer Electrolyte $\beta$ -PEO<sub>6</sub>:LiAsF<sub>6</sub>



27 non-H atoms  
*JACS* 127 (2005), 12176-12177  
*E. Staunton, Yu. G. Andreev, and P. G. Bruce*

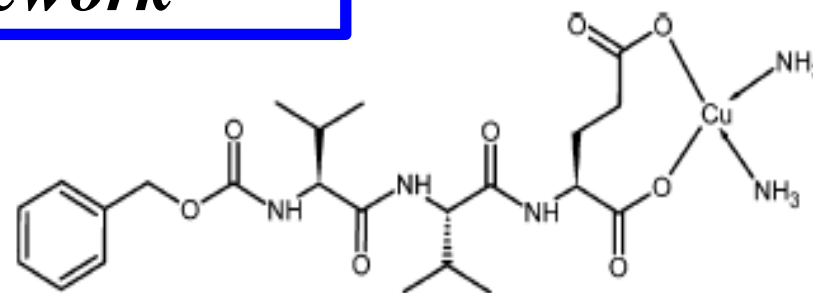




# Metal-Peptide Framework

**JACS (02/2008) DOI:10.1021/ja0762588**

A. Manton, L. Massüger, P. Rabu, C. Palivan,  
L. B. McCusker & A. Taubert



**37 independent atoms**

**~ 20 internal DOF, 1 flexible 9-atom ring**

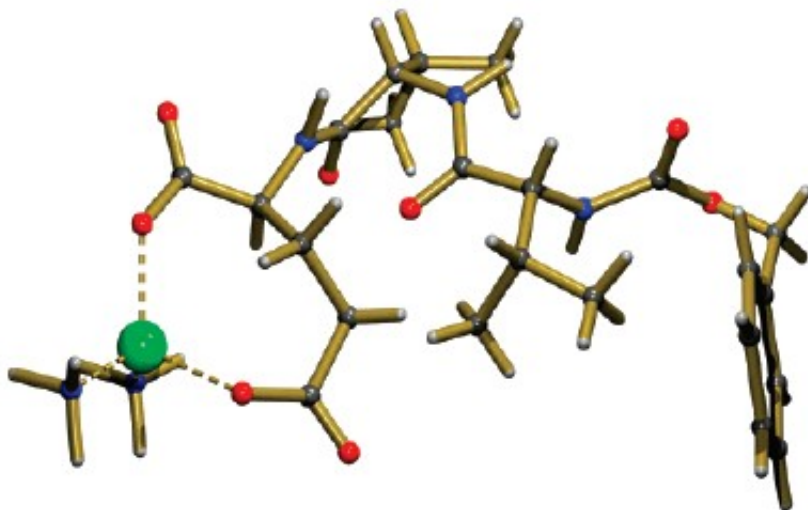


Figure 9. Crystal structure of MPF-9 generated by FOX and before Rietveld refinement, including hydrogen atoms.

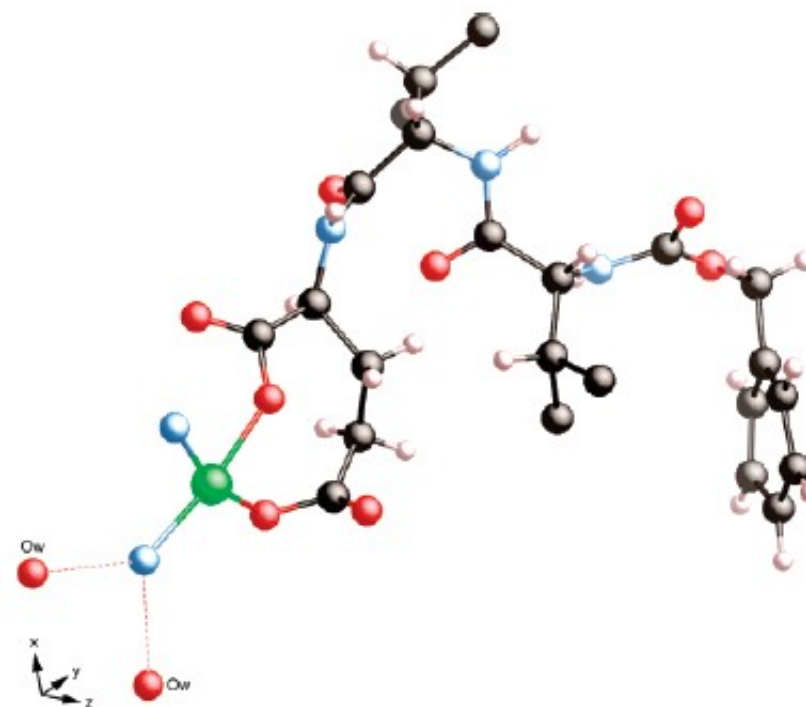
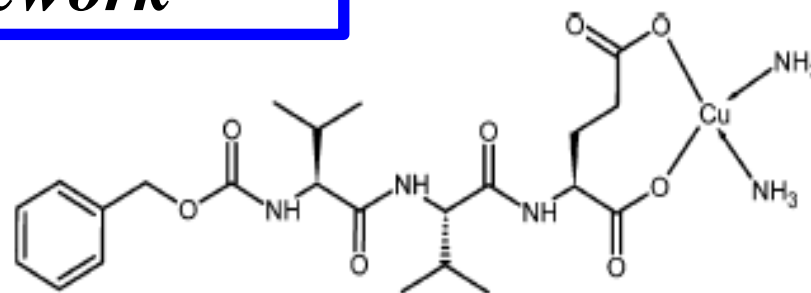


Figure 10. Crystal structure of MPF-9 after refinement of the model generated by FOX, including the water molecule.

# Metal-Peptide Framework

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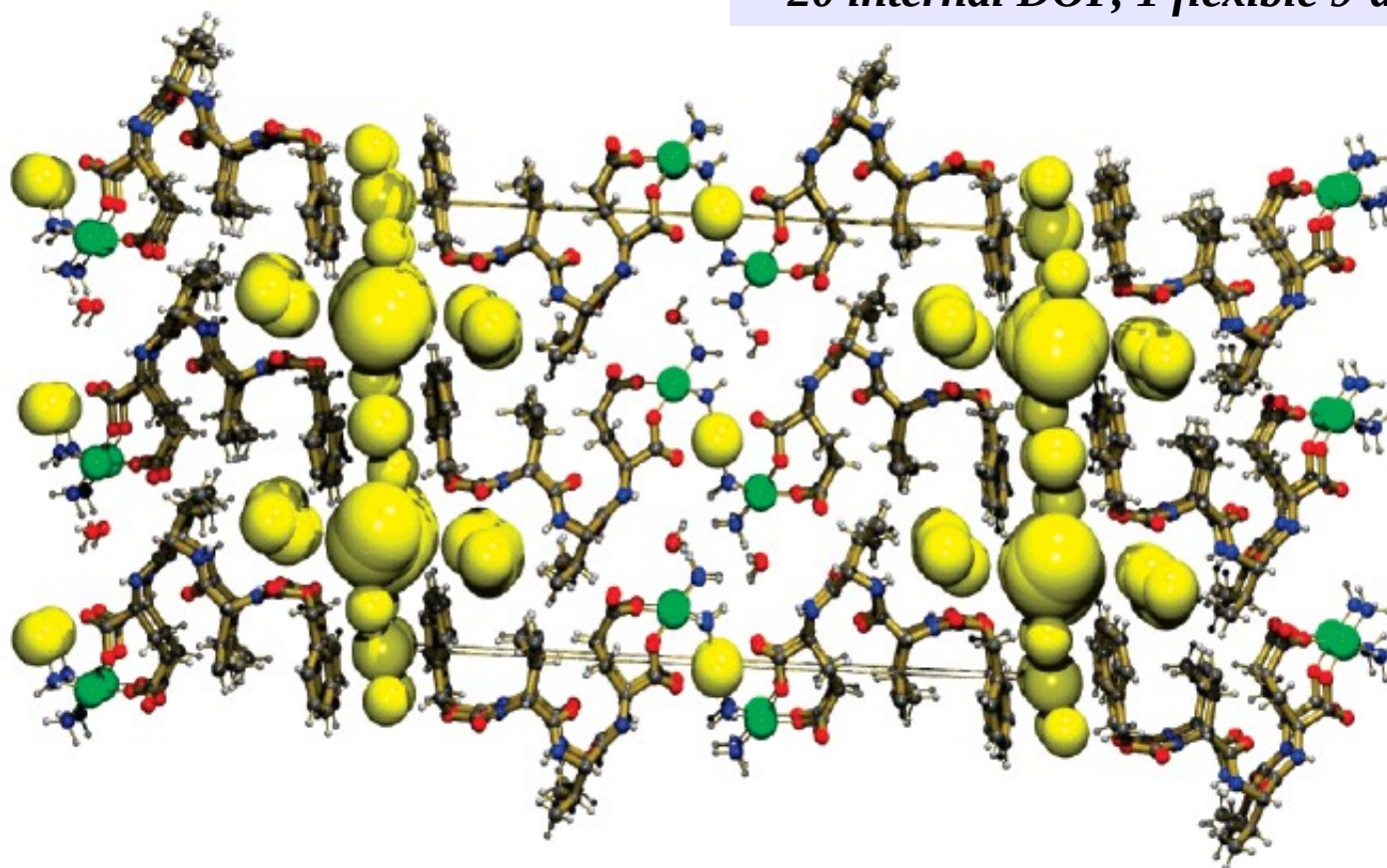


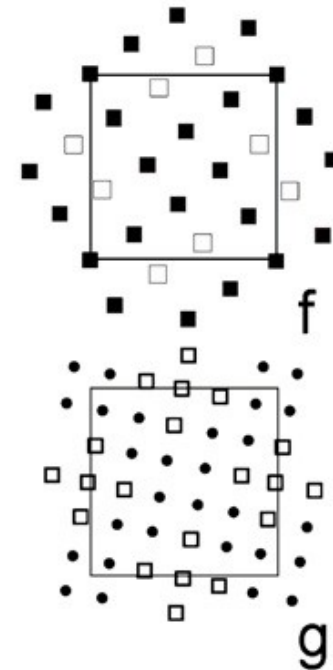
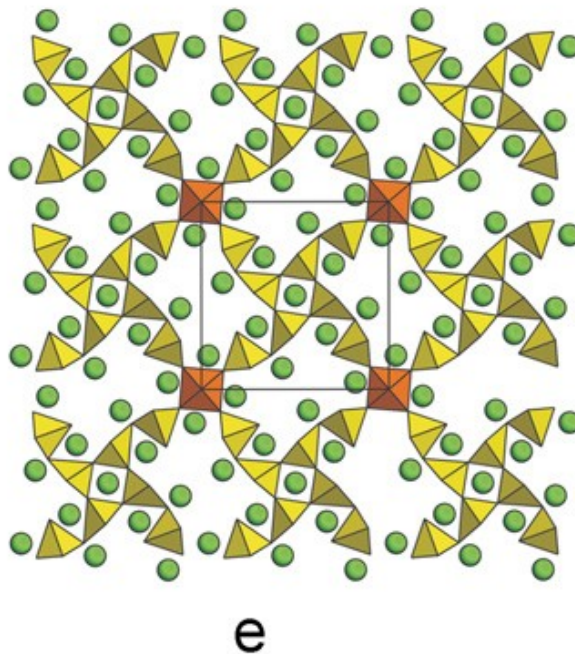
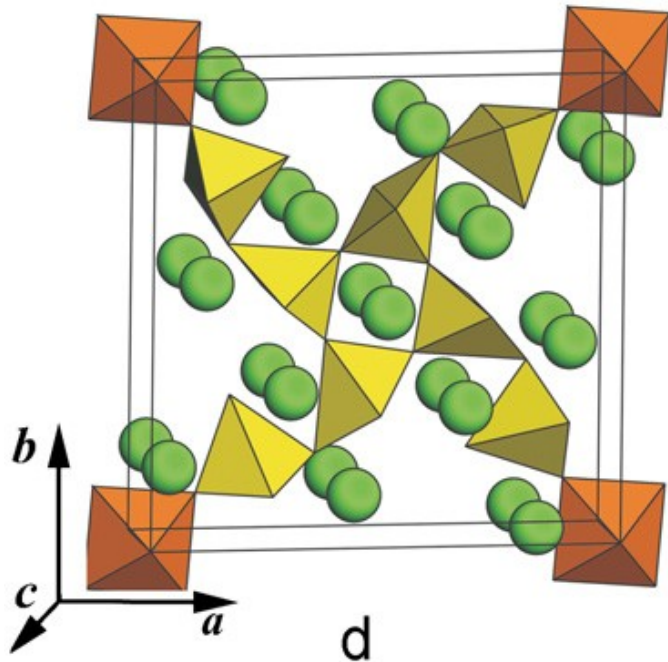
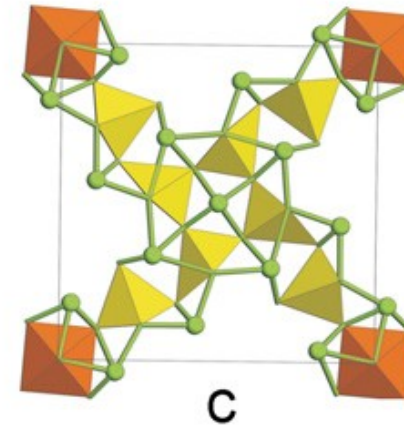
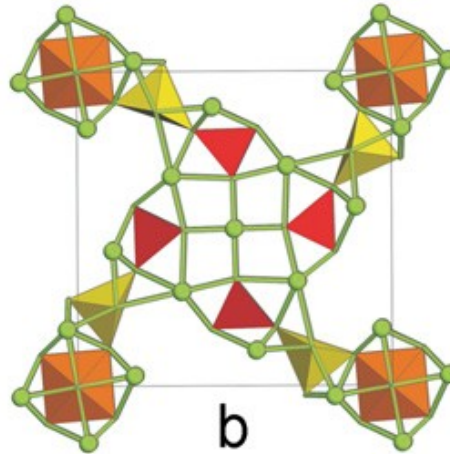
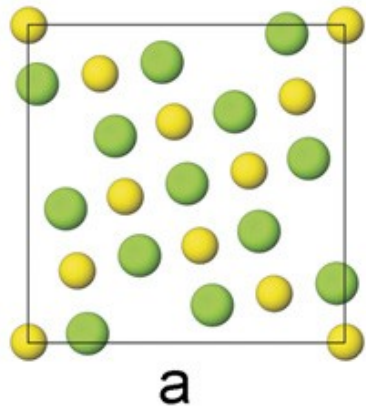
Figure 15. Packing diagram of MPF-9. Yellow balls indicate the voids.

# Electron diffraction

$\text{Pb}_{13}\text{Mn}_9\text{O}_{25}$  precession electron diffraction data  
 $P4/m, Z = 1$

J. Hadermann et al., *Ultramicroscopy* **110** (2010) 881–890

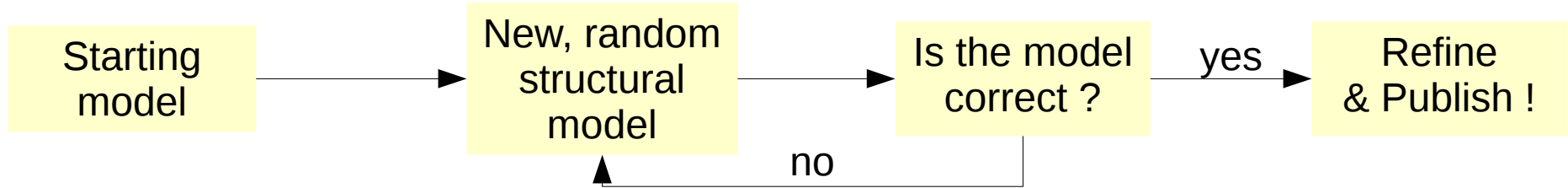
- a) Pb and Mn from direct methods (SIR2008)  
b,c) O localized by FOX using:  
- antibumps  
- BVS cost function  
c,d) Rietveld and DFT  
confirmed the correct model





# Real-Space Exploration ?

## Basic Direct-space Algorithm (trial & error):



A good program requires :

... this works but is only adequate for the very patient crystallographer !

**Criteria** to test the validity of the the model

**An ergodic algorithm** which:

- can explore **every possible** structural model
- will spend more time "close" to the real solution (efficient **biasing**)

**A flexible modeling of the structure:**

- allowing to reduce the number of parameters (**Degrees of Freedom**)
- able to describe any structure
- allow easy configuration changes

# ***Criteria for Minimization***

# Criteria to Evaluate Trial Structural Models

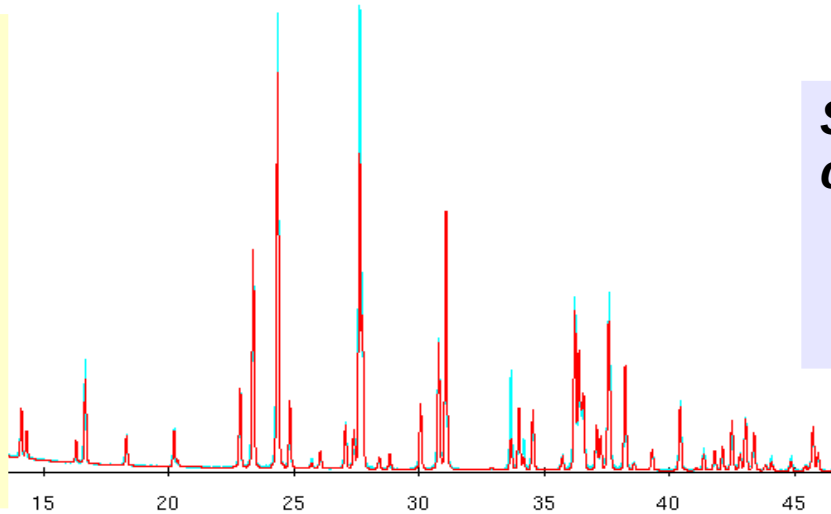
## Diffraction Data

### R-factor

$$R_{wp} = \sqrt{\frac{\sum w_i (I_i^{obs} - I_i^{calc})^2}{\sum w_i (I_i^{obs})^2}}$$

or  $c^2$

$$\chi^2 = \sum \frac{1}{\sigma_i^2} (I_i^{obs} - I_i^{calc})^2$$

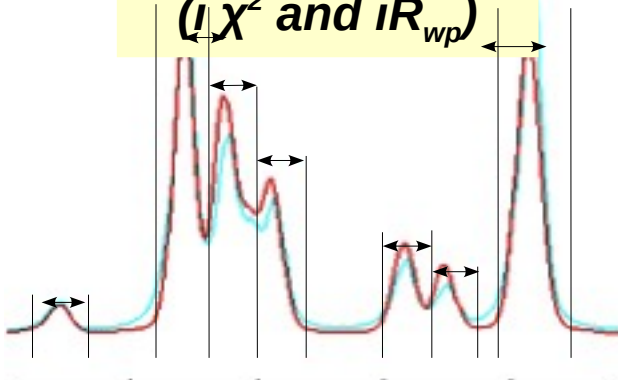


Several datasets can be combined:

X-rays & neutrons  
several wavelengths,  
Several temperatures ...

### integrated profiles

( $i\chi^2$  and  $iR_{wp}$ )



Integrated profiles allow to avoid the requirement of a perfect description of profiles

Why not use extracted structure factors (faster & equivalent) ?

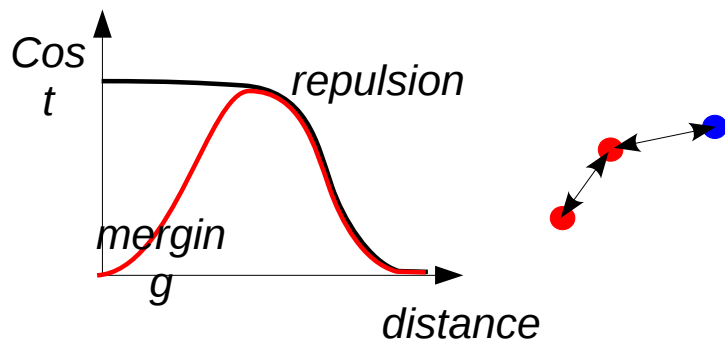
- This would require a **perfect description** of the profiles and background, which can be difficult ("real" samples, with ill profiles and multiple phases, background difficult to "guess" for close-packed reflections).
- Direct-space algorithms are necessary for samples where the extraction of structure factors is difficult
- with "integrated profiles", the full pattern is not calculated and the speed is equivalent to extracted structure factors



# Criteria to Evaluate Trial Structural Models

## AntiBump Restraint

### Anti-bump



An **AntiBump** function allows the repulsion of atoms while permitting the “merging” of identical atoms on special positions or connecting several polyhedra

### Energy calculations ?

*Either internal energy for molecules or  
global for the entire unit cell*

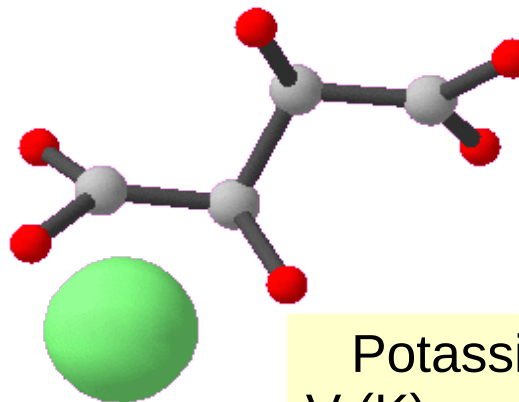
*... But energy calculations are extremely  
costly from a computation point of view*

# Criteria to Evaluate Trial Structural Models

## Bond Valence

$$V_i = \sum_{\text{neighbours } j} e^{\frac{(R_1 - r_{ij})}{0.37}}$$

**The valence of each atom depends on its neighbours and their distance :**



Potassium tartrate :  
 $V(K)_{\text{calc}} = + 0.991$  OK!

**Warning:** bond valence / AntiBump calculations use a lot of computing power (as much or more than structure factor computation)

=> only use them if the diffraction data is not of sufficient quality to solve the structure

# Criteria to Evaluate Trial Structural Models

## Combining Several Criteria

**Problem: different criteria will have different scales !!**

**When combining experimental data,  $\chi^2$  can be summed:**

$$\chi^2 = \sum_{data\ 1} \frac{1}{\sigma_i^2} (I_i^{obs} - I_i^{calc})^2 + \sum_{data\ 2} \frac{1}{\sigma_i^2} (I_i^{obs} - I_i^{calc})^2 + \dots$$

**=> avoid using R-factors which cannot be summed**

**Fringe benefit: using  $\chi^2$  makes you ready for maximum likelihood (ML)**

Sometimes combining « incompatible » criteria ( $\chi^2$ , energy, antibump) is necessary  
=> finding the correct scale can be difficult.

=> correct scale factors can be guess if you know the 'target' values :

e.g.  $\chi^2$  should converge towards **Nobs** (Goodness-Of-Fit=1), antibump towards 0, etc..

Sometimes scaling different data sets is necessary (e.g. combine powder diffraction data from synchrotron and neutron) : statistically, no scale should be applied, but for « global optimisation » algorithms rules may be bent (see later ML slides)

# ***Model Building: Real Space Parametrization***

# Structural Description from Building Blocks: the Z-matrix approach

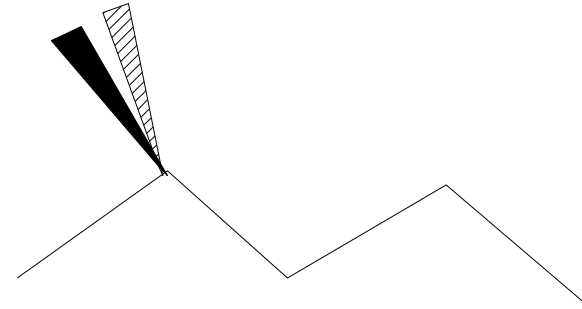
*The number of trials required  
varies exponentially with the  
number of parameters*

*=> need to use all the a priori  
information about the atomic  
coordination*

*Building blocks for  
the crystal  
structure*



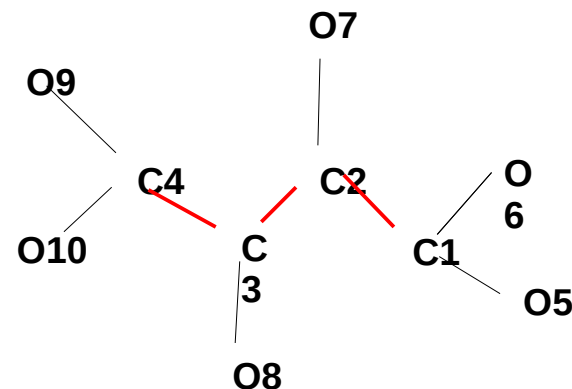
*atom*



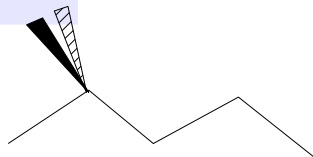
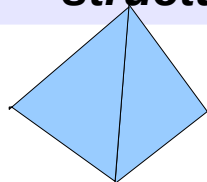
# Structural Description from Building Blocks: the Z-matrix approach

The number of trials required varies exponentially with the number of parameters

=> need to use all the a priori information about the atomic coordination



Building blocks for the crystal structure



atom

Polyhedron

molecule

Description from bond lengths, bond angles and dihedral angles

Z-Matrix

10	← number of atoms				
C	1				
C	1	1.5			
C	2	1.5	1	110	
C	3	1.5	2	110	<b>1 0</b>
O	1	1.2	2	120	<b>3 0</b>
O	1	1.2	2	120	5 180
O	2	1.4	1	110	<b>3 180</b>
O	3	1.4	2	110	<b>4 180</b>
O	4	1.2	3	120	<b>2 0</b>
O	4	1.2	3	120	9 180

atom type

free torsion angles

bond length with atom #

bond angle with atom #

dihedral angle with atom #

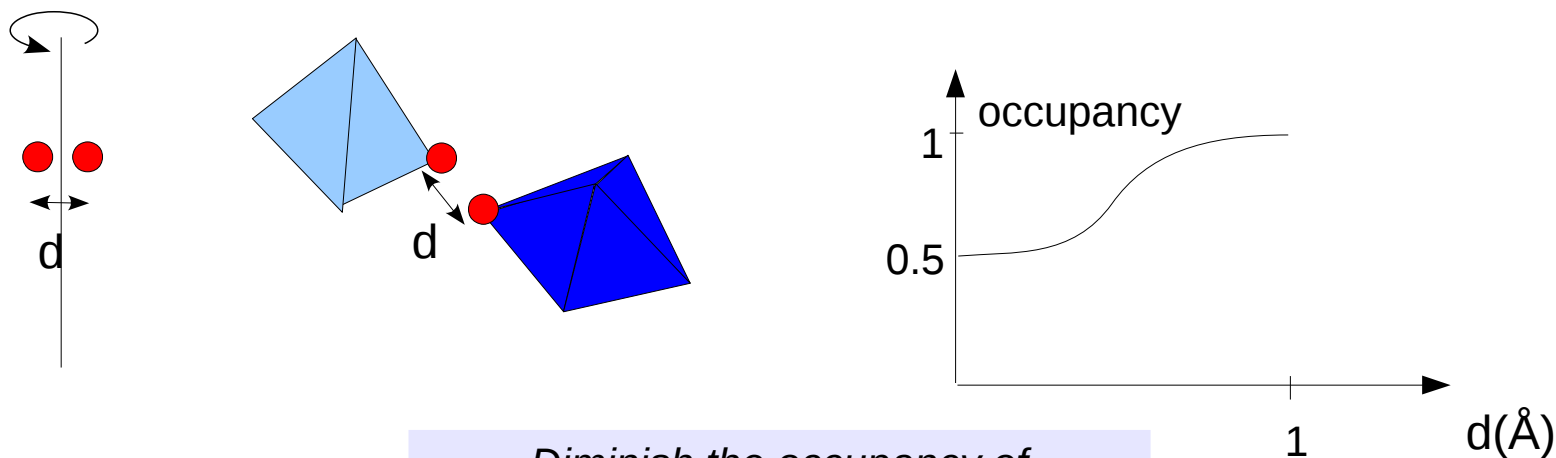
**30 -> 6+5=11 DOF**



# Dynamical Occupancy Correction

Inorganic structures often have atoms in **special positions**, and have **atoms common to several polyhedra**. => New algorithm which must:

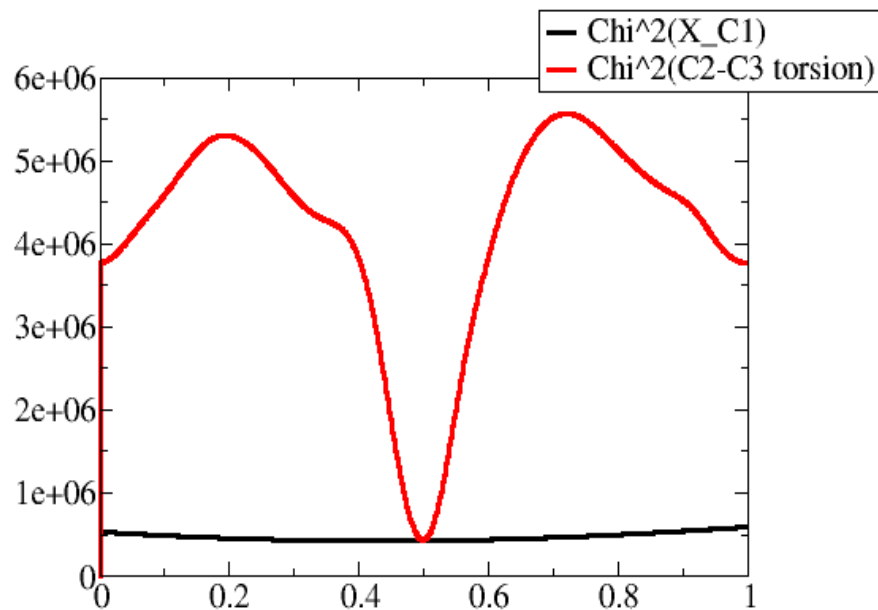
- correctly describe atoms in special positions **without a priori knowledge**
- allow the atoms to move continuously to and from the special positions
- not depend on the type of compound or the modelling chosen (atoms, polyhedra, molecules)



Diminish the occupancy of overlapping atoms as they are getting closer

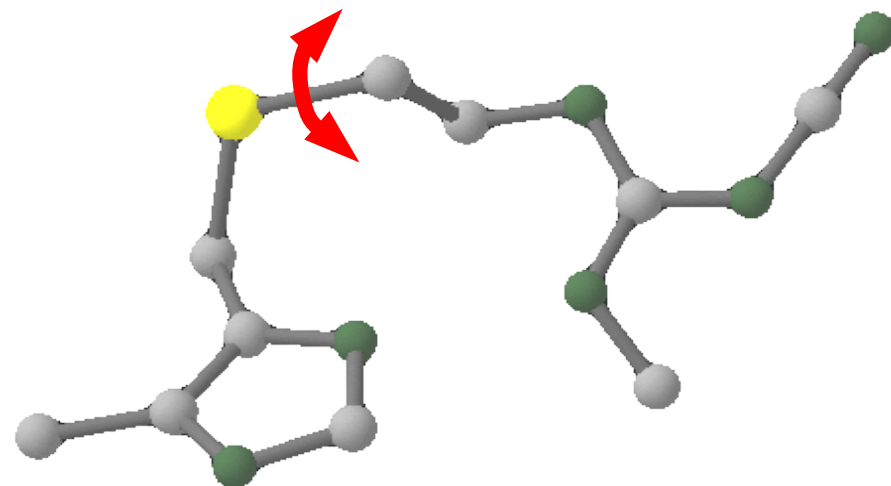
**! Warning !** Do not use the DOC if no special positions or shared atoms are expected, as it slows down the computation.

# Pitfalls of internal coordinates (z-matrix)



a **torsion angle** (moving many atoms) has a **much narrower minimum** than a translation parameter of an individual atom

=> even if the number of degrees of freedom diminishes, the global minimum is much narrower



Atoms are deduced from previous atoms  
=> the first atoms in the z-matrix must also be the first to be found

=> **The convergence can depend on the order of the atoms in the z-matrix**

The z-matrix approach reduces the parameter space to explore, but makes it (much) more difficult to find the solution

# Flexible Approach using Restraints

*idea: keep all the coordination information, but with a **flexible approach***

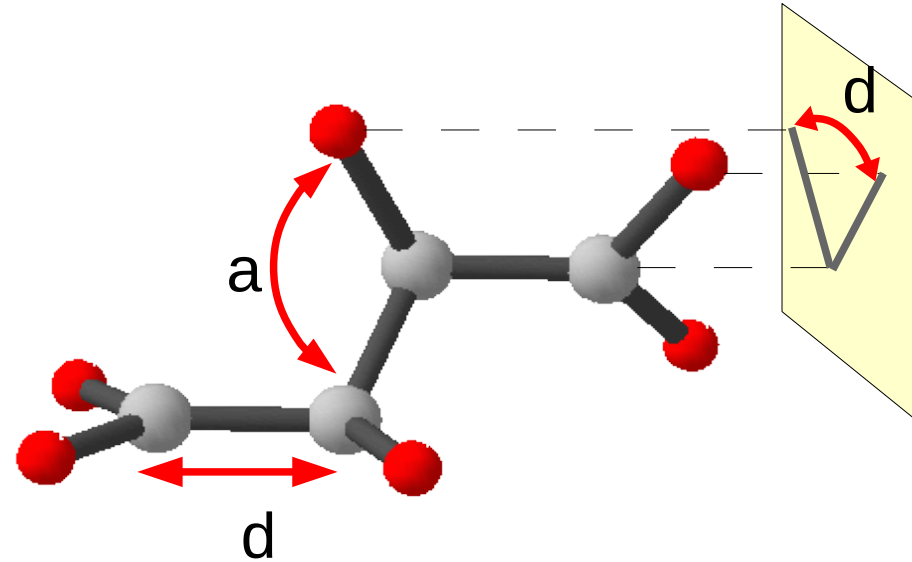
All atom positions are directly defined by their **xyz** coordinates

**and**

the coordination information is introduced by **restraints** on:

- **bond lengths**  $\chi^2 = \frac{(d - d_0)^2}{\sigma_d^2}$
- **bond angles**  $\chi^2 = \frac{(\alpha - \alpha_0)^2}{\sigma_\alpha^2}$
- **dihedral angles**

The orientation of the molecule is defined by a **quaternion** (to avoid "gimbal lock" angles)

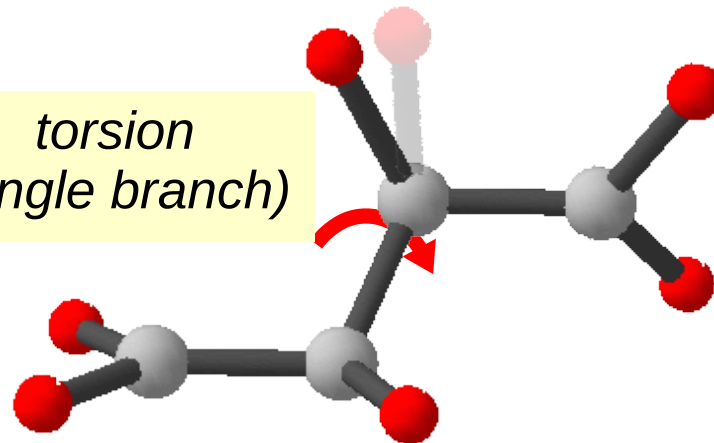


- this modelization is **independent from the order of the atoms**
- **any type of restraint** can be introduced
- **any type of movement** can be directly done (no need to compute complex torsions)
- **any cycle** can be defined

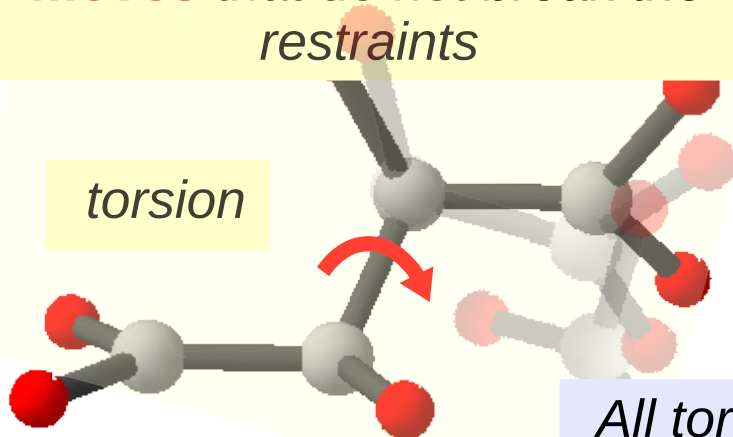
# Making the Smart Moves

With atoms defined independently, it is vital to have **intelligent moves** that do not break the restraints

torsion  
(single branch)

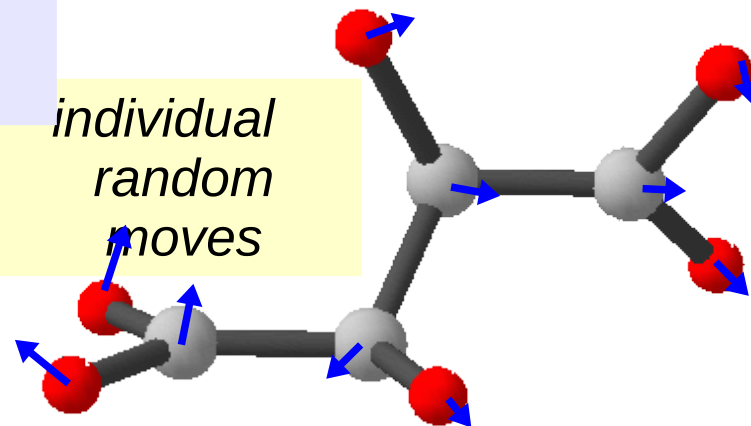


torsion

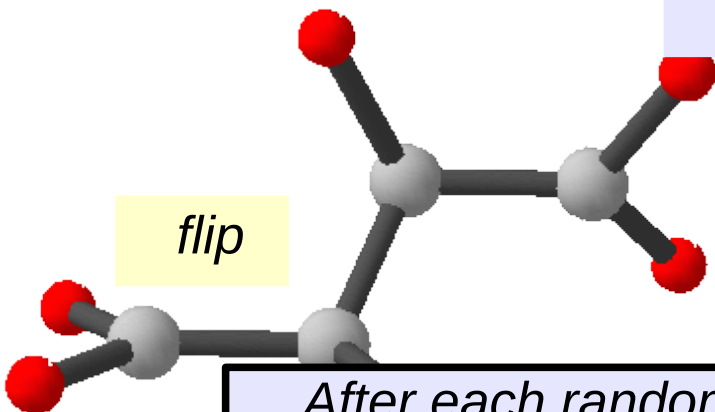


All torsion & flip moves that do not break restraints are **automatically identified**

individual  
random  
moves



flip

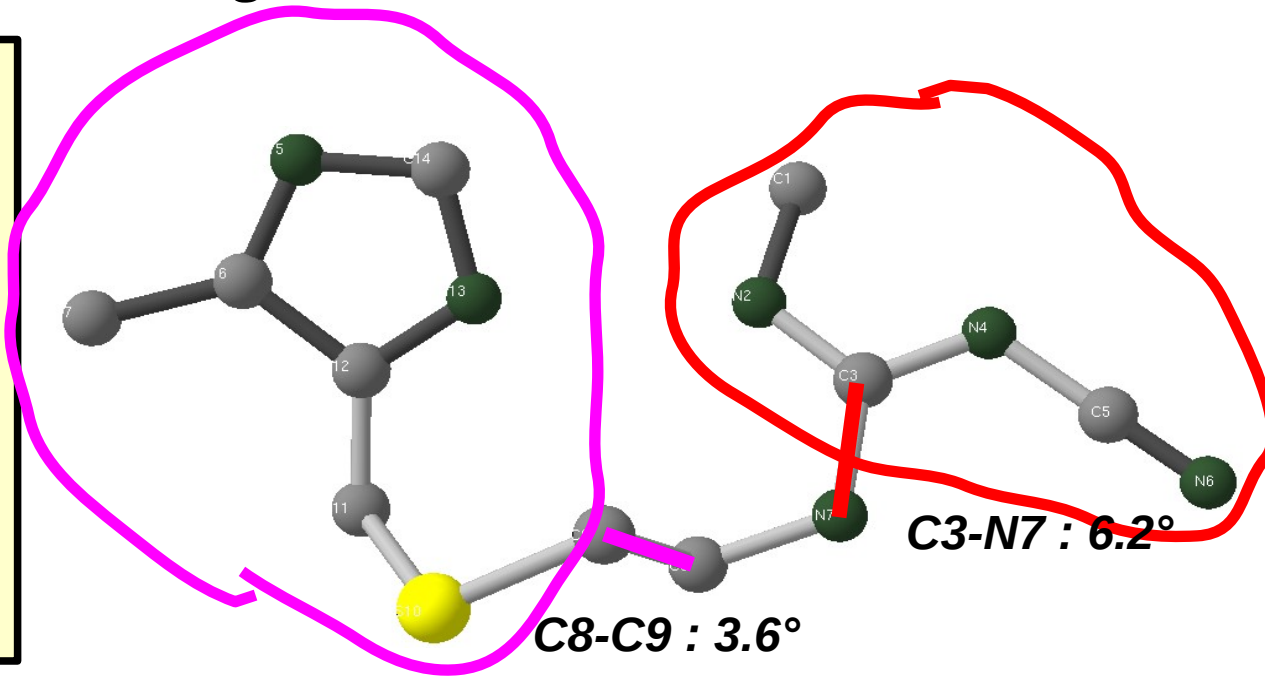


After each random move, a test is made on the total internal restraint cost to see if the configuration is kept

# Adaptative Conformation Changes

**Random torsion angle changes :**

- rotate the **smallest fragment**
- **tune the max. rotation** so that the **average displacement is 0.1Å.**
- same for bond angle changes
- tune global rotation of molecule

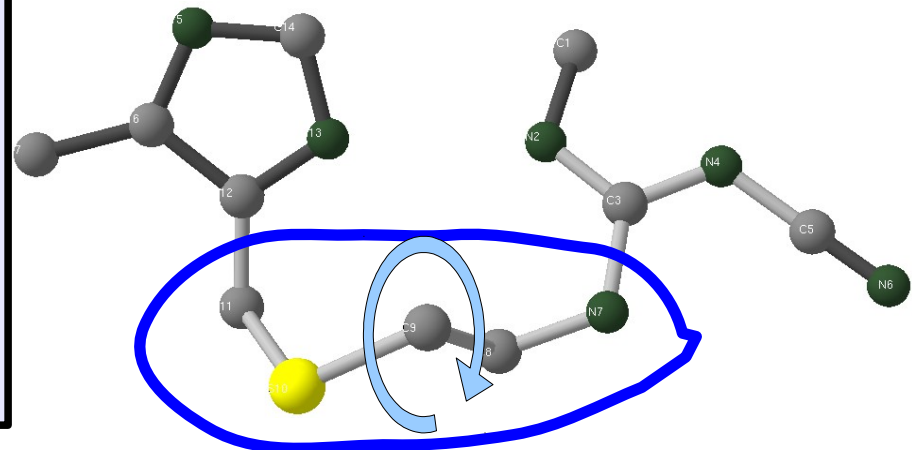


**“ Twist ” mode :**

alter an **internal** part of a chain/cycle

=> long chains, flexible cycles

**TODO:** determine “ **soft modes** ” of the molecule and use them to distort the molecule (computationally costly)



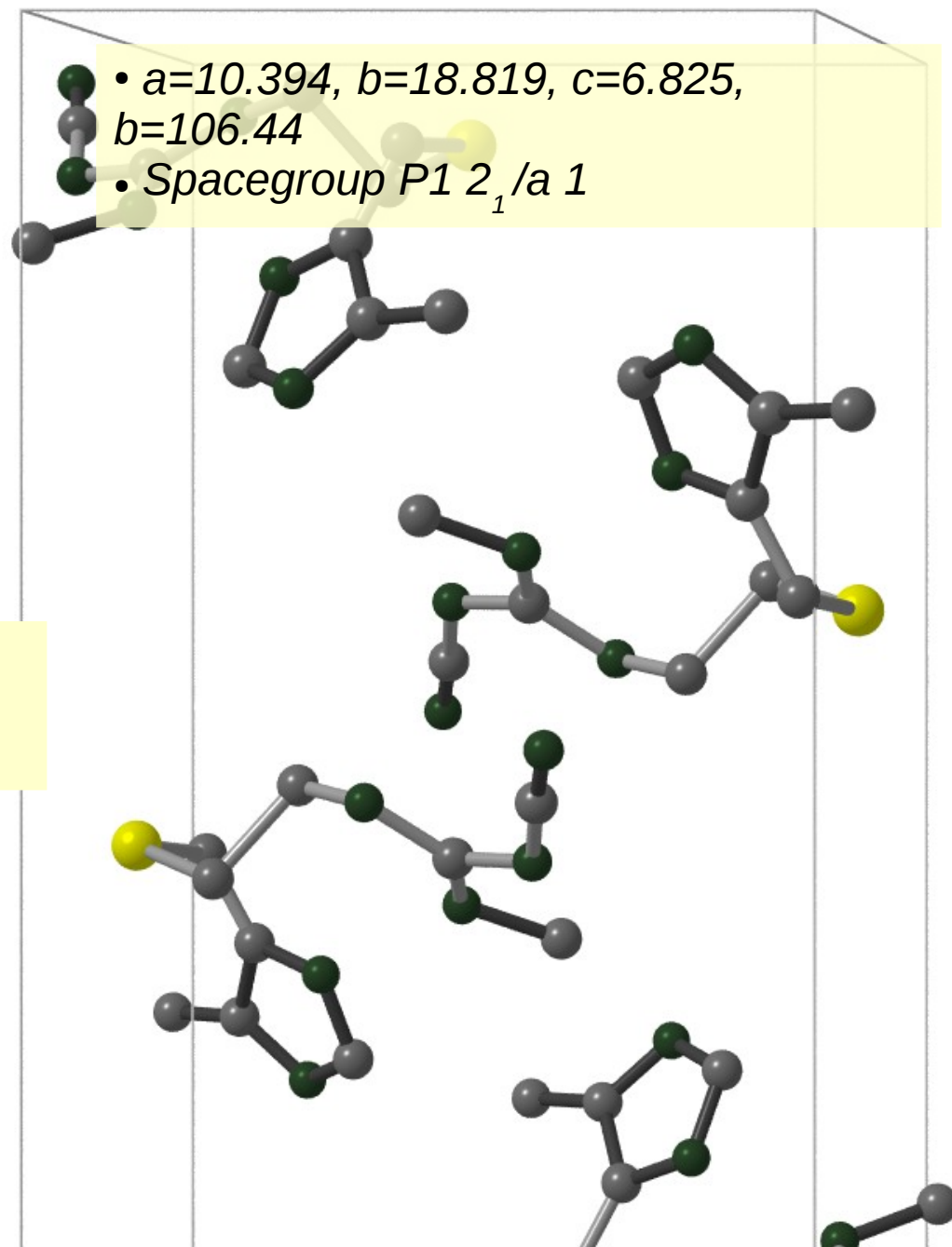
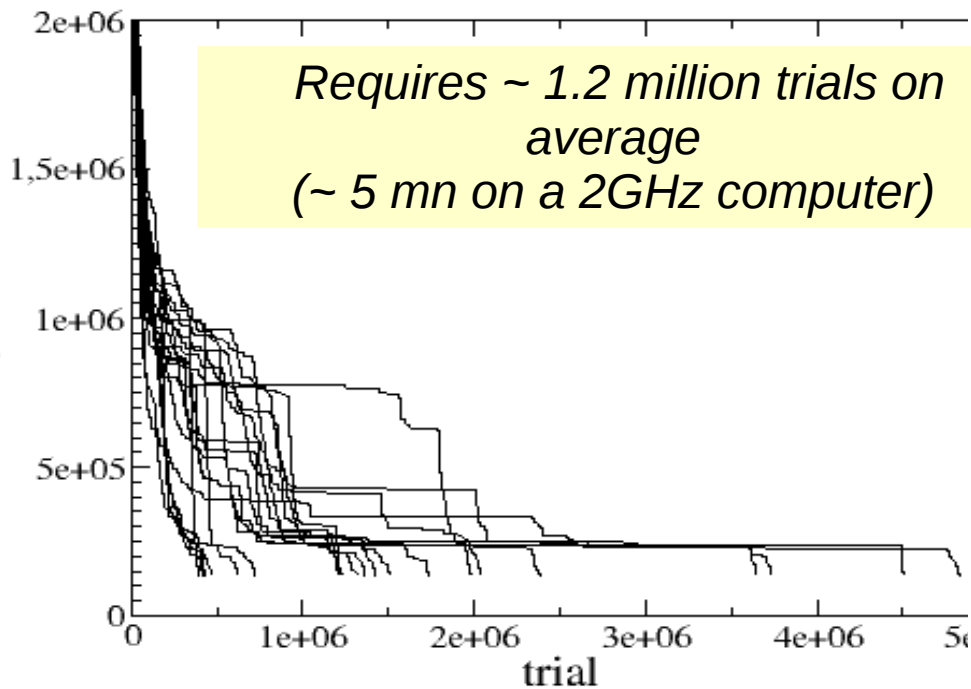
# Cimetidine

A well-known testcase for ab initio structure determination from powder diffraction

17 non-H atoms (8+6=14 DOF)

Cernik et al. *J. Appl. Cryst* **24** (1991), 222

**Results : up to 3 times faster than with the z-matrix model**





# Reverse Monte-Carlo

Parametrization  
-> *Degrees Of Freedom*

starting configuration

random change of parameters

evaluation of the new configuration:  
*Cost (C)*

is configuration better?  
 $C_n < C_{n-1}$

keep configuration with probability:

$$P = e^{\frac{-\Delta C}{T}}$$

*Temperature*  
of the algorithm

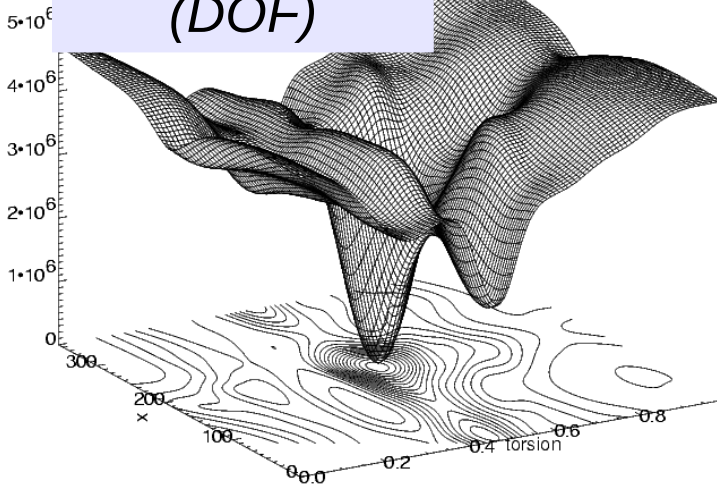
Generate a *distribution of configurations* following **Boltzmann's law**

keep configuration

yes

no

Hypersurface  
 $Cost = f$   
(DOF)



# Reverse Monte-Carlo

Parametrization  
-> *Degrees Of Freedom*

starting configuration

random change of parameters

evaluation of the new configuration:  
*Cost (C)*

is configuration better?  
 $C_n < C_{n-1}$

keep configuration with probability:

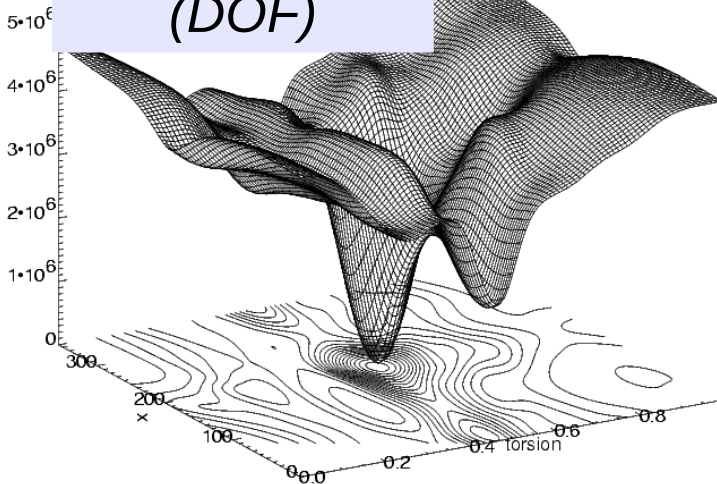
$$P = e^{-\frac{\Delta C}{T}}$$

*Temperature*  
of the algorithm

Generate a *distribution configurations* following **Boltzmann's law**

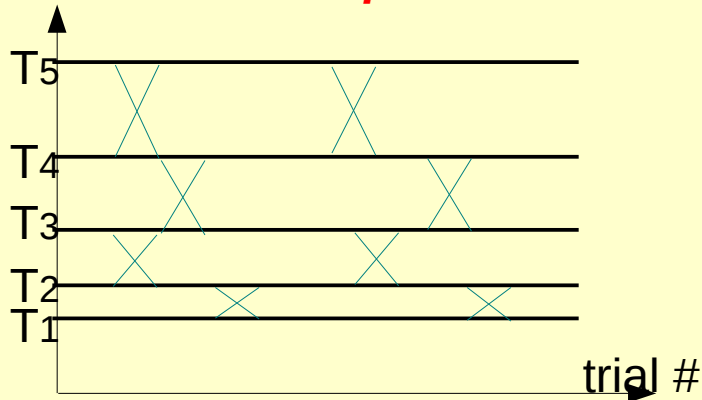
**Simulated Annealing** :  
decrease  $T$  as a function of the trial number to converge towards the global minimum

Hypersurface  
 $Cost = f$   
(DOF)



# Parallel Tempering & Annealing Temperatures

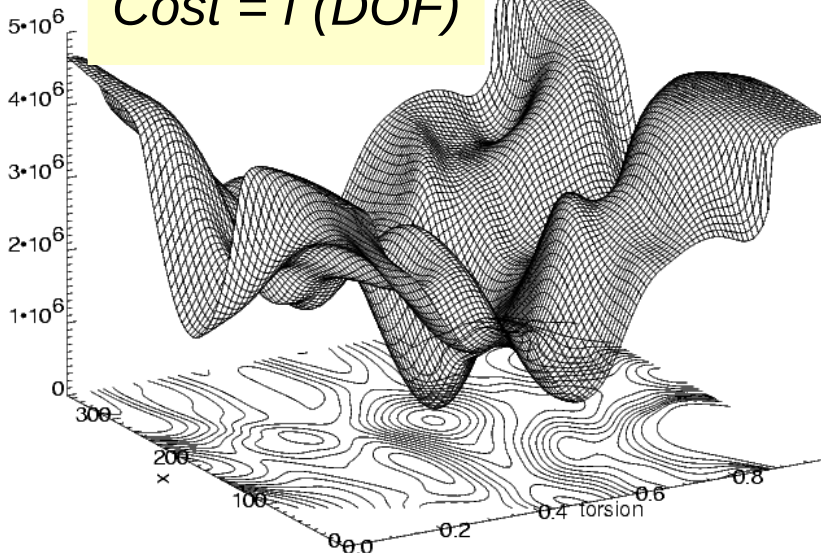
simultaneous optimization  
at **different temperatures**



Using several parallel optimizations at different temperatures ensures that **the algorithm can get out of any local minimum.**

Furthermore, it does not require to predict an adequate decrease rate for the temperature.

Hypersurface  
Cost =  $f(\text{DOF})$



To automatically choose the temperatures, in each parallel optimization **it is the average atomic displacement per random move which is imposed, from 0.01 to 1 Å.**

The Temperature is then tuned so that in each “world” **the acceptance rate of new configurations is from 10 to 30%.**

# ***Maximum Likelihood & Global Optimization***

# Maximum Likelihood

**WARNING :**

**Approximations !**  
(Theorists hold your fire !)

In a "classical approach" :

$$\sigma^2 = y_{obs}$$

$$\chi^2 = \sum \frac{(y_{obs}^i - y_{calc}^i)^2}{\sigma_i^2}$$

assumes that the model can fit **perfectly** the observed data.  
But there can be **errors** in the model !

typically **positionnal errors** during the search for a structure solution

with a positionnal error measured by:  $D(\vec{k}) = \langle \cos(2\pi \vec{k} \cdot \Delta \vec{r}) \rangle$

introduce a **variance** on the  
calculated structure factor

$$\sigma_{calc}^2 = (1 - D^2) \sum_{atoms} f_j^2$$

Use the "**most likely**"  
calculated structure factor

$$\langle F_{calc} \rangle = DF_{calc}$$

$$\sigma_i^2 = \sigma_{calc}^2 + \sigma_{obs}^2$$

$$\chi^2 = \sum \frac{(y_{obs}^i - \langle y_{calc}^i \rangle)^2}{\sigma_i^2}$$

# Application to Global Optimization

1<sup>st</sup> application:  
**incomplete model**

missing atoms ( H's, solvant) do not contribute to the **Structure Factor** but increase the **variance**

$$D(\vec{k}) = \langle \cos(2\pi \vec{k} \cdot \Delta \vec{r}) \rangle = 0$$

$$\langle F_{calc} \rangle = DF_{calc} = 0$$

$$\sigma_{calc}^2 = (1 - D^2) \sum_{atoms} f_j^2$$

Markvardsen, Acta Cryst  
A58(2002)

2<sup>nd</sup> application:  
**model errors**

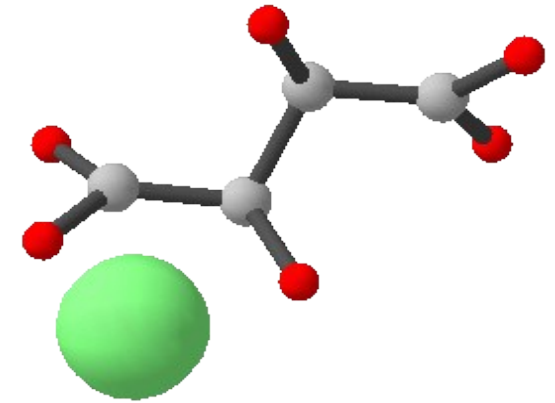
**Atoms are always misplaced during a global optimisation**

taking into account **random positional errors** should yield a **better agreement between the incorrect model and the observed diffraction data**

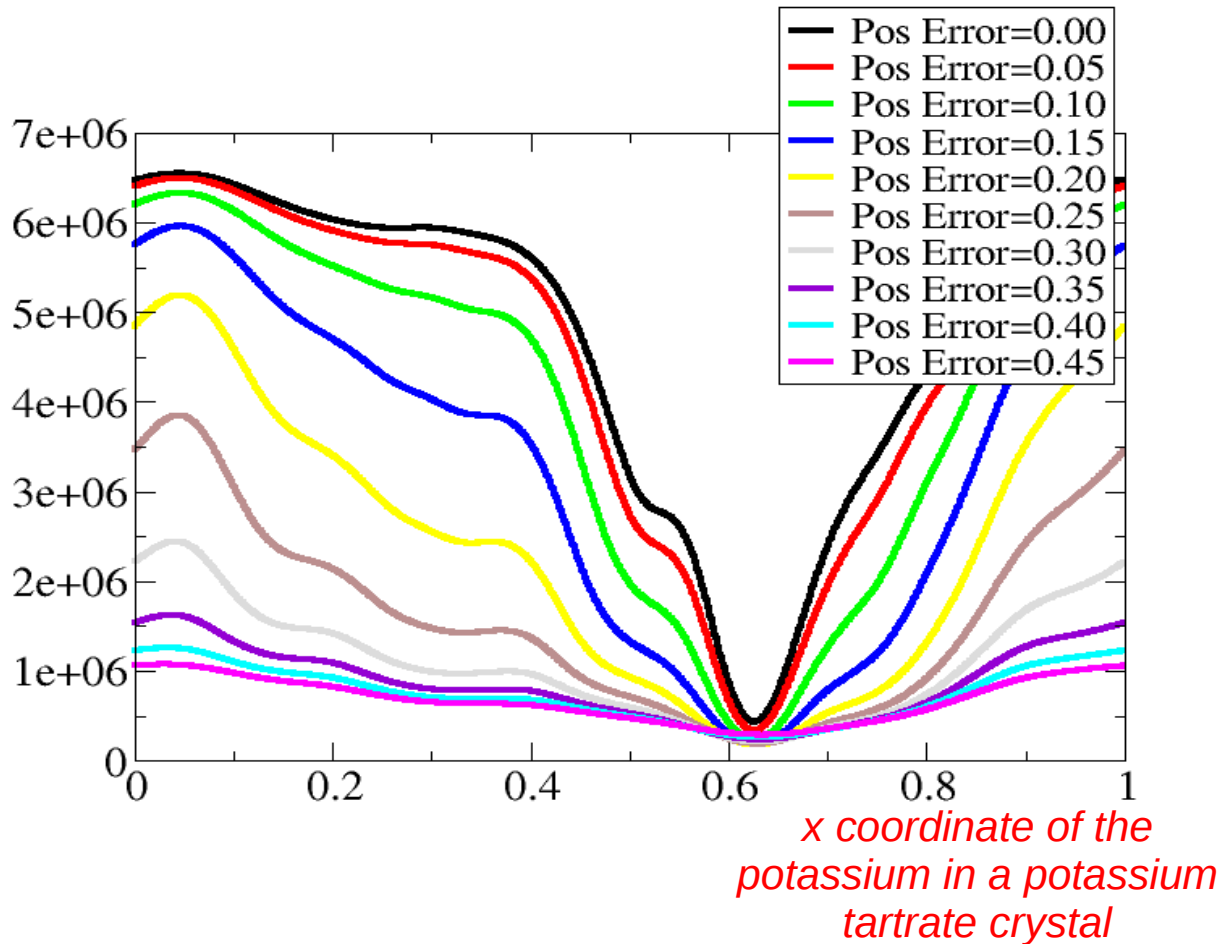
can it help its **convergence** ?



# Hypersurface as a function of positionnal error



Hypersurface:  $\chi^2 = f(\text{parameters})$



taking into account  
random positionnal errors:

- **increases the width of the global minimum** (for small errors)
- **flattens the hypersurface** for large errors

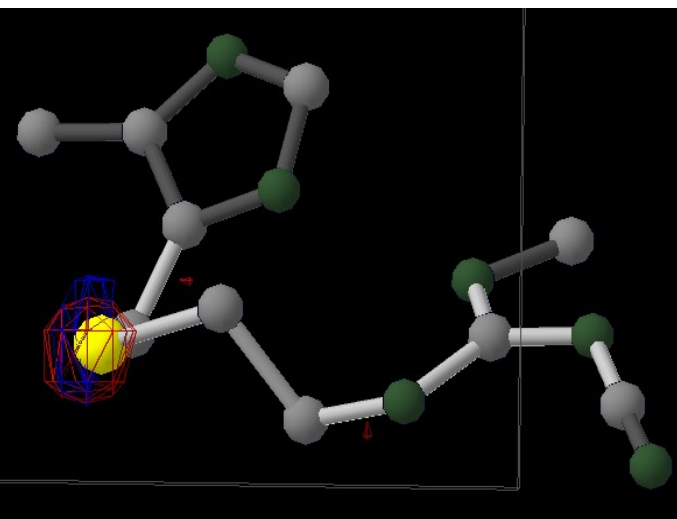
# Rules to find a structure solution: check multiple solutions

Look at multiple solutions => estimate confidence in  
" solution "

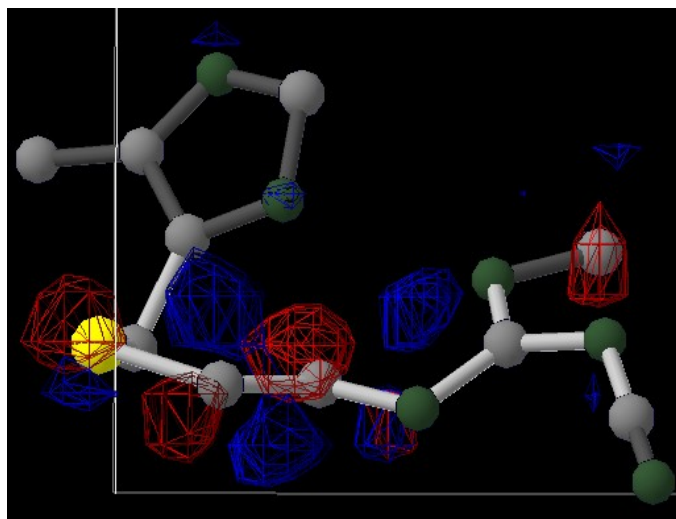
1) Compare the  $\chi^2$  and Rwp

2) Use **Fourier Difference Maps** to check differences  
(requires at least 1.5Å resolution data)

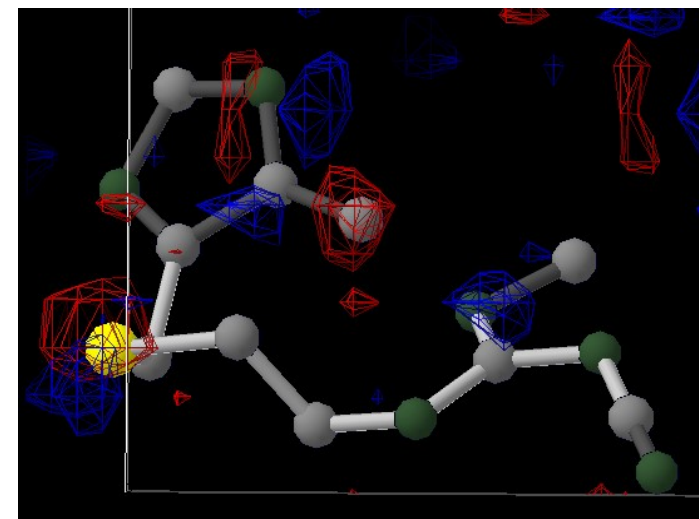
Use the same contours for all solutions  
*Fo-Fc, +1 and -1 contours*



**Correct**



**Wrong conformation  
of internal chain**



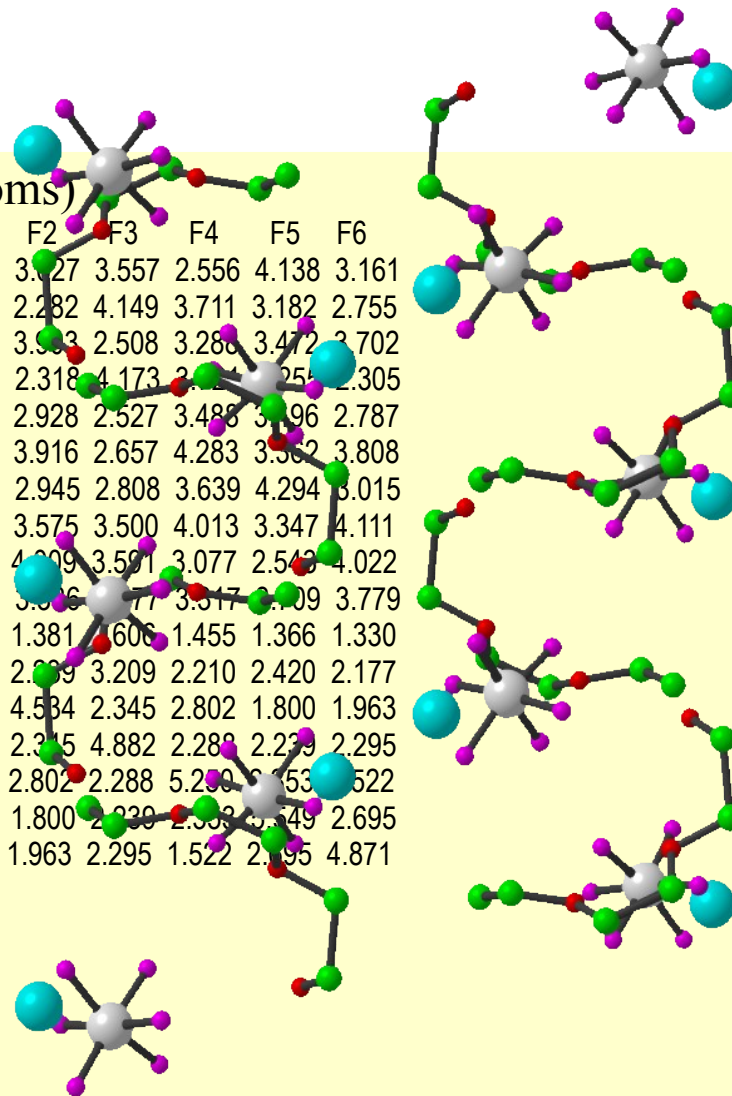
**Wrong position  
for side CH<sub>3</sub> group**

# Interatomic distances

Check distances, overlap between atoms

Table of minimal distances between all components (atoms)

	Li	C5	C6	O3	C4	C3	O2	C2	C1	O1	As	F1	F2	F3	F4	F5	F6
Li	5.380	3.455	3.689	2.300	2.659	3.079	2.661	1.219	1.727	2.865	3.693	2.889	3.627	3.557	2.556	4.138	3.161
C5	3.455	5.160	1.571	1.436	2.322	3.469	3.530	3.789	3.074	1.829	3.175	2.389	2.282	4.149	3.711	3.182	2.755
C6	3.689	1.571	5.059	2.475	3.670	4.275	2.969	3.044	2.123	0.874	4.048	3.447	3.903	2.508	3.288	3.472	3.702
O3	2.300	1.436	2.475	4.893	1.471	2.472	2.959	2.781	3.687	3.165	2.873	3.612	2.318	4.173	2.251	2.305	2.305
C4	2.659	2.322	3.670	1.471	4.174	1.522	2.426	3.003	3.962	4.098	2.890	3.827	2.928	2.527	3.488	3.496	2.787
C3	3.079	3.469	4.275	2.472	1.522	2.890	1.349	2.428	3.481	3.958	4.383	3.754	3.916	2.657	4.283	3.362	3.808
O2	2.661	3.530	2.969	2.959	2.426	1.349	3.693	1.457	2.435	2.707	4.101	3.683	2.945	2.808	3.639	4.294	3.015
C2	1.219	3.789	3.044	2.781	3.003	2.428	1.457	4.955	1.067	2.379	4.260	3.606	3.575	3.500	4.013	3.347	4.111
C1	1.727	3.074	2.123	3.687	3.962	3.481	2.435	1.067	4.115	1.391	3.271	3.844	4.009	3.591	3.077	2.543	4.022
O1	2.865	1.829	0.874	3.165	4.098	3.958	2.707	2.379	1.391	4.398	4.048	3.344	3.346	3.517	3.509	3.779	3.779
As	3.693	3.175	4.048	2.873	2.890	4.383	4.101	4.260	3.271	4.048	5.570	1.607	1.381	1.606	1.455	1.366	1.330
F1	2.889	2.389	3.447	3.612	3.827	3.754	3.683	3.606	3.844	3.344	1.607	3.077	2.239	3.209	2.210	2.420	2.177
F2	3.627	2.282	3.903	2.318	2.928	3.916	2.945	3.575	4.009	3.336	1.381	2.239	4.534	2.345	2.802	1.800	1.963
F3	3.557	4.149	2.508	4.173	2.527	2.657	2.808	3.500	3.591	3.077	1.606	3.209	2.345	4.882	2.288	2.239	2.295
F4	2.556	3.711	3.288	3.721	3.488	4.283	3.639	4.013	3.077	3.317	1.455	2.210	2.802	2.288	5.250	2.553	3.522
F5	4.138	3.182	3.472	3.255	3.496	3.362	4.294	3.347	2.543	3.709	1.366	2.420	1.800	2.239	2.553	2.549	2.695
F6	3.161	2.755	3.702	2.305	2.787	3.808	3.015	4.111	4.022	3.779	1.330	2.177	1.963	2.295	1.522	2.195	4.871



*Polymer Electrolyte  $\beta$ -PEO<sub>6</sub>:LiAsF<sub>6</sub>*

E.Staunton, Yu. Andreev, P. Bruce *JACS* 127 (2005), 12176

# Top problems for *ab initio* structure determination:

(assuming data and unit cell correctly)

## #1 Model is wrong:

- wrong formula
- incorrect restraints
- wrong spacegroup
- missing solvant
- ...

### Solution:

- 1- check **real** composition (mass spectroscopy, EDX microscope)
- 2- Add new atoms/polyhedra if they are missing

(The first structure solved with Fox,  $\text{CsOH}\cdot\text{H}_2\text{O}$   
...was supposed to be a Cs hydride !)

## #2 Preferred Orientation

### Solution:

- 1- Collect new data
- ...
- 9- Collect new data
- 10- Search for preferred orientation parameters *ab initio*

Phys. Rev. B 76 (2007), 092104

## #3 Not enough data

### Solution:

Add more restraints: antibump, bond length  
Use other methods to gather restraints (NMR)

## #4 Need a faster computer ?

Check with literature if more trials are really required  
or email the author for advice !

## **Rules to find a structure solution: be a flexible User**

*Restraints must be used to reduce parameter space*

*... but **too many restraints** can **slow** or **prevent** a structure solution*

*e.g.: a combination of strong antibump and angular restraints can make very difficult to go from one local minimum to the global one.*

*Imagine the “molecule” to be solved is: a man & a chair.*

*The “solution” is:*

*the man, sitting on the chair, in the Prado Museum (Madrid)*

*The random starting location is: Grenoble railway station.*

*To “speed up” the solution, you impose as much restraints as you can, i.e. “the man must be sitted on the chair at all times”*

*=> Rigid groups should be used scarcely... and do not generally speed up the convergence*

*=> **if the algorithm “distorts” your molecule during the optimization, it's for your own good (honest !)***

*=> the correct conformation comes from the data, not the number of restraints  
=> NB: different rules apply if data is of bad quality*

## **Rules to find a structure solution: no high-resolution data**

*“ Solving the structure ” means finding all the atomic positions with an error of ~  
0.1Å.*

*=> high resolution data (1Å and higher) is not needed...  
increasing the resolution by 25% doubles the computing time !*

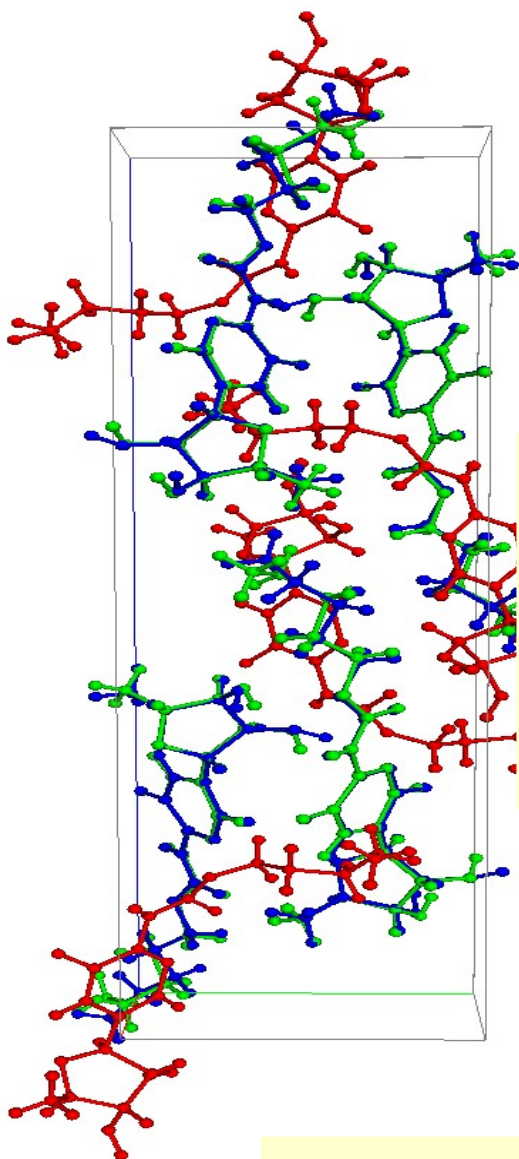
*Giving high-resolution data is like giving your address to a friend  
....by insisting on the **exact pattern of colours from your garden's flowers**  
... instead of **just giving the address & colour** of the house*

*Most of the time, a 2.5 Å resolution is  
enough.  
...sometimes 1.5Å.*

*Of course you still need the high-resolution data for the least squares  
refinement !*



# Comparing crystal structures



CrystalCMP

File Similarity

0: OptimizationObj #02009-03-18\_00-54-25-Run#1-Cost-431625.875000.xml  
1: OptimizationObj #02009-03-18\_01-01-57-Run#1-Cost-138774.718750.xml  
2: OptimizationObj #02009-03-18\_10-59-45-Cost-70584.320313.xml  
3: OptimizationObj #02009-03-18\_11-49-45-Cost-54914.210938.xml  
4: OptimizationObj #02009-03-18\_12-49-45-Cost-50931.828125.xml  
5: OptimizationObj #02009-03-18\_13-49-45-Cost-49458.351563.xml  
6: OptimizationObj #02009-03-18\_14-39-45-Cost-47199.054688.xml  
7: OptimizationObj #02009-03-18\_15-49-45-Cost-47199.050781.xml  
8: OptimizationObj #02009-03-18\_16-39-45-Cost-47199.046875.xml

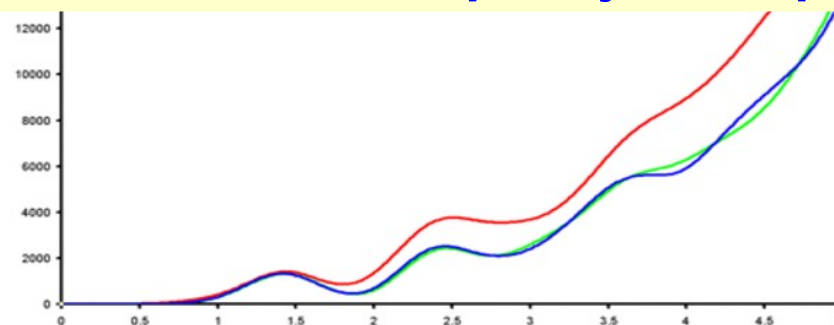
ID	Comput	Show	Move
0	TRUE	TRUE	FALSE
1	TRUE	TRUE	FALSE
2	TRUE	TRUE	FALSE
3	TRUE	FALSE	FALSE
4	TRUE	FALSE	FALSE
5	TRUE	FALSE	FALSE
6	TRUE	FALSE	FALSE
7	TRUE	FALSE	FALSE
8	TRUE	FALSE	FALSE

FingerPrint similarity

ID	0	1	2	3	4	5	6	7
0:	0.000	0.334	0.333	0.319	0.293	0.324	0.318	0.318
1:	0.334	0.000	0.040	0.043	0.049	0.036	0.048	0.048
2:	0.333	0.040	0.000	0.024	0.049	0.022	0.024	0.024
3:	0.319	0.043	0.024	0.000	0.033	0.015	0.018	0.018
4:	0.293	0.049	0.049	0.033	0.000	0.036	0.038	0.038

**Sometimes the score ( $\chi^2$ , Rwp) is not enough to decide which solution is correct**

**=> to browse among solutions a tool has been developed (Jan Rohlíček, Michal Hušák, ICT Prague):**  
<http://crystalcmp.sf.net>



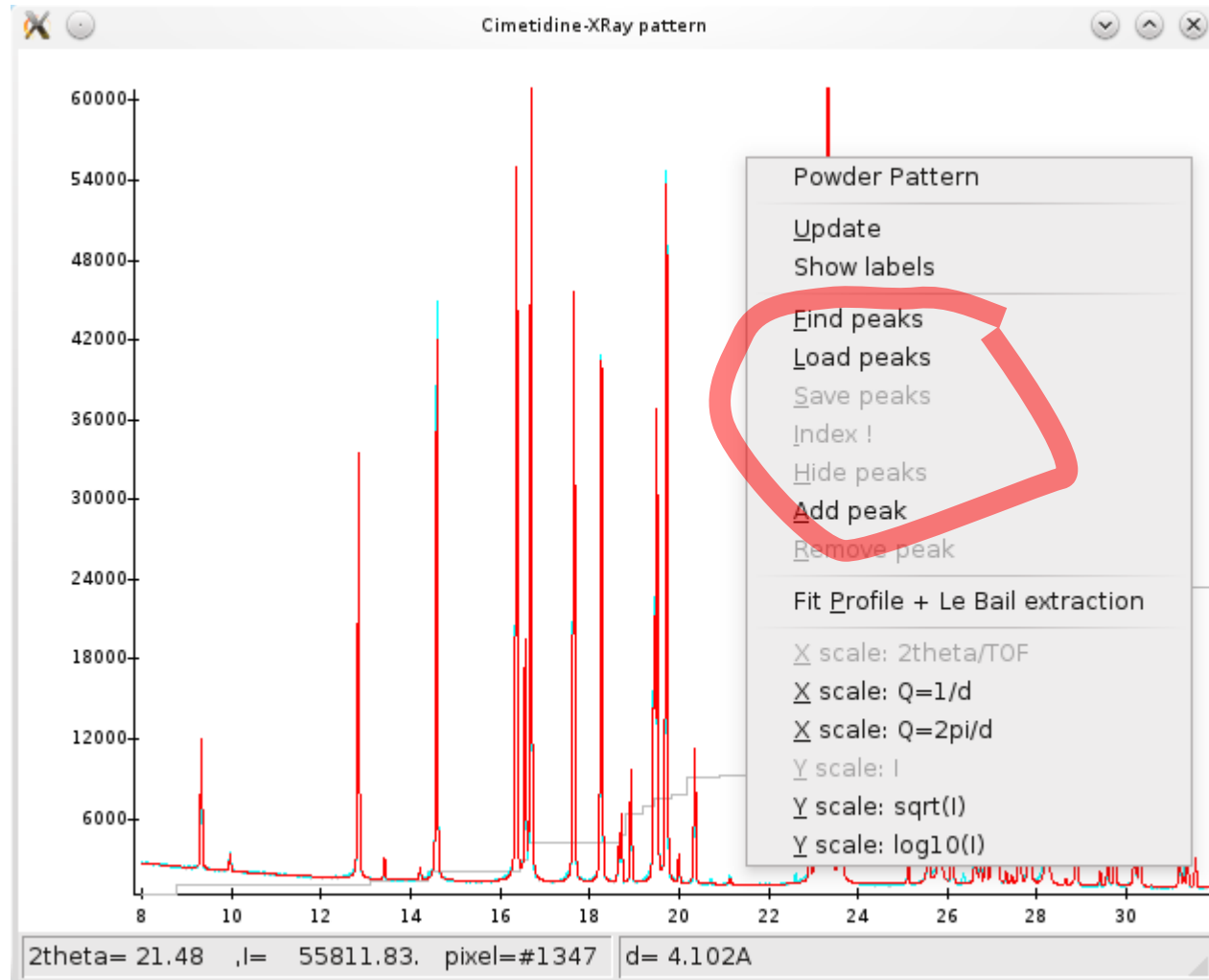
**=> allows to superpose several structures**  
**=> also compares a 'fingerprint' of all molecules**

# ***Fox: recent features***



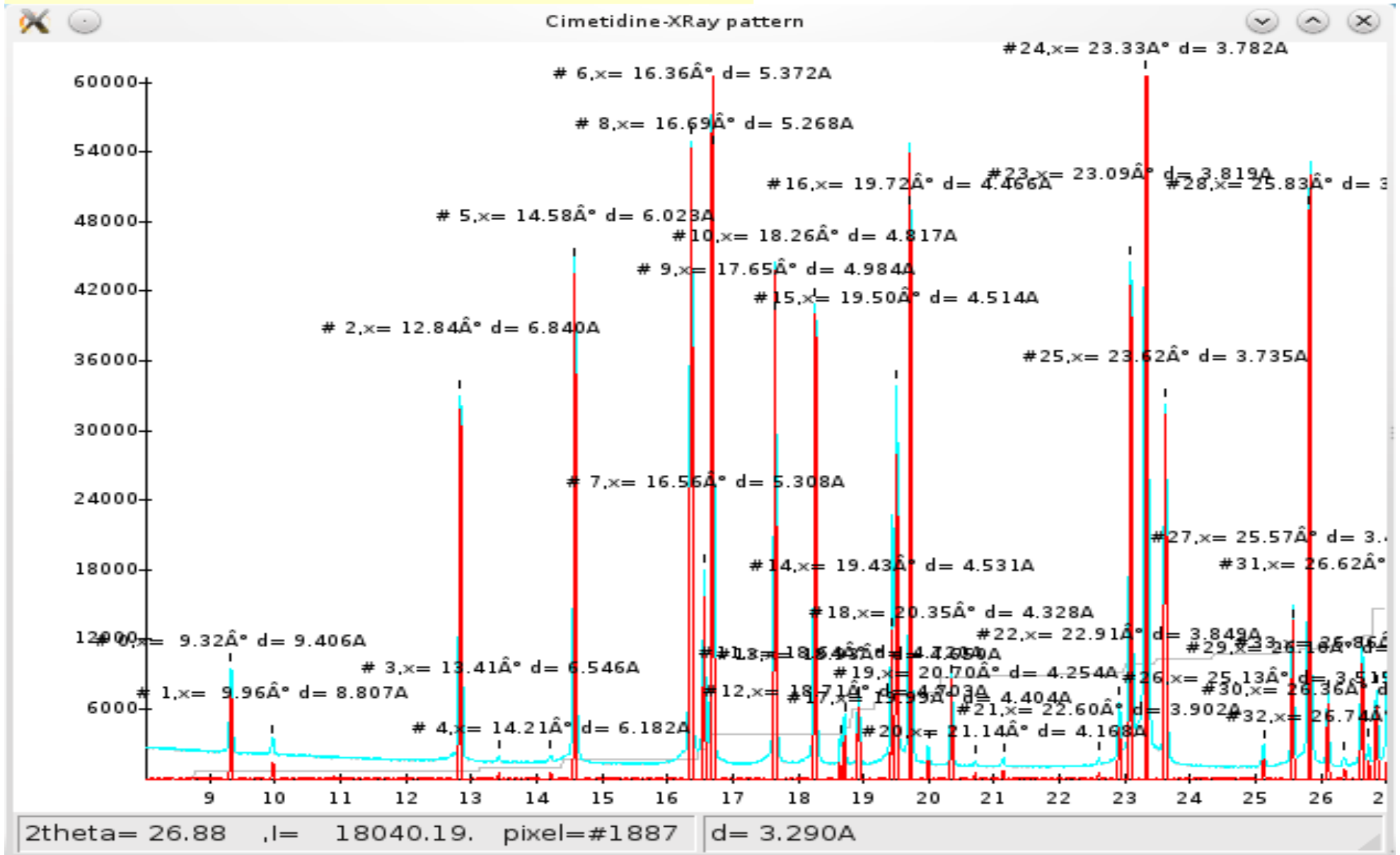
# Auto-indexing

- Search for peaks



# Auto-indexing

- Search for peaks



# Auto-indexing

Choose crystal to apply selected cell to: Choose crystal to apply select

Automatic Profile Fitting (Le Bail)

Score	V	a	b	c	$\alpha$	$\beta$	$\gamma$	System
130.4	1281.0	1.0	6.827	18.820	10.394	90.00	106.43	MONOCLINIC P
130.2	1281.0	1.0	10.700	18.820	10.394	90.00	142.27	MONOCLINIC P
130.2	1281.0	1.0	10.394	18.820	10.700	90.00	142.27	MONOCLINIC P
130.1	1281.0	1.0	6.827	18.820	10.700	90.00	111.30	MONOCLINIC P
98.6	2561.2	2.0	13.652	18.818	14.633	90.00	137.05	MONOCLINIC P
98.6	2561.2	2.0	10.394	18.818	13.652	90.00	106.43	MONOCLINIC P
98.6	2561.2	2.0	10.394	18.818	14.633	90.00	116.51	MONOCLINIC P
98.5	2561.2	2.0	14.633	18.818	13.652	90.00	137.05	MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P
90.00						90.00		MONOCLINIC P

Predicting volumes from 20 peaks between  $d=94.058$  and  $d= 4.254$   
Starting indexing using 20 peaks

System	V	$A^3$	max length	sols in	time	best score
CUBIC P	4699	34122	97.30A	0	0.19s	0.0
TETRAGONAL P	1744	8923	62.22A	0	0.04s	0.0
RHOMBOEDRAL	1932	9448	63.42A	0	0.08s	0.0
HEXAGONAL	2382	12321	69.29A	0	0.09s	0.0
ORTHOROMBIC P	1014	4714	50.30A	1	0.09s	7.7
MONOCLINIC P	756	3099	43.74A	1	0.09s	130.1

Finished indexing, bestscore= 130.1, elapsed time= 0.62s

Predicting volumes from 20 peaks between  $d=94.058$  and  $d= 4.254$   
Starting indexing using 20 peaks

System	V	$A^3$	max length	sols in	time	best score
CUBIC P	4699	34122	97.30A	0	0.18s	0.0
TETRAGONAL P	1744	8923	62.22A	0	0.08s	0.0
RHOMBOEDRAL	1932	9448	63.42A	0	0.02s	0.0
HEXAGONAL	2382	12321	69.29A	0	0.06s	0.0
ORTHOROMBIC P	1014	4714	50.30A	1	0.09s	7.7
MONOCLINIC P	756	3099	43.74A	14	2.76s	130.2

Finished indexing, bestscore= 130.2, elapsed time= 3.28s

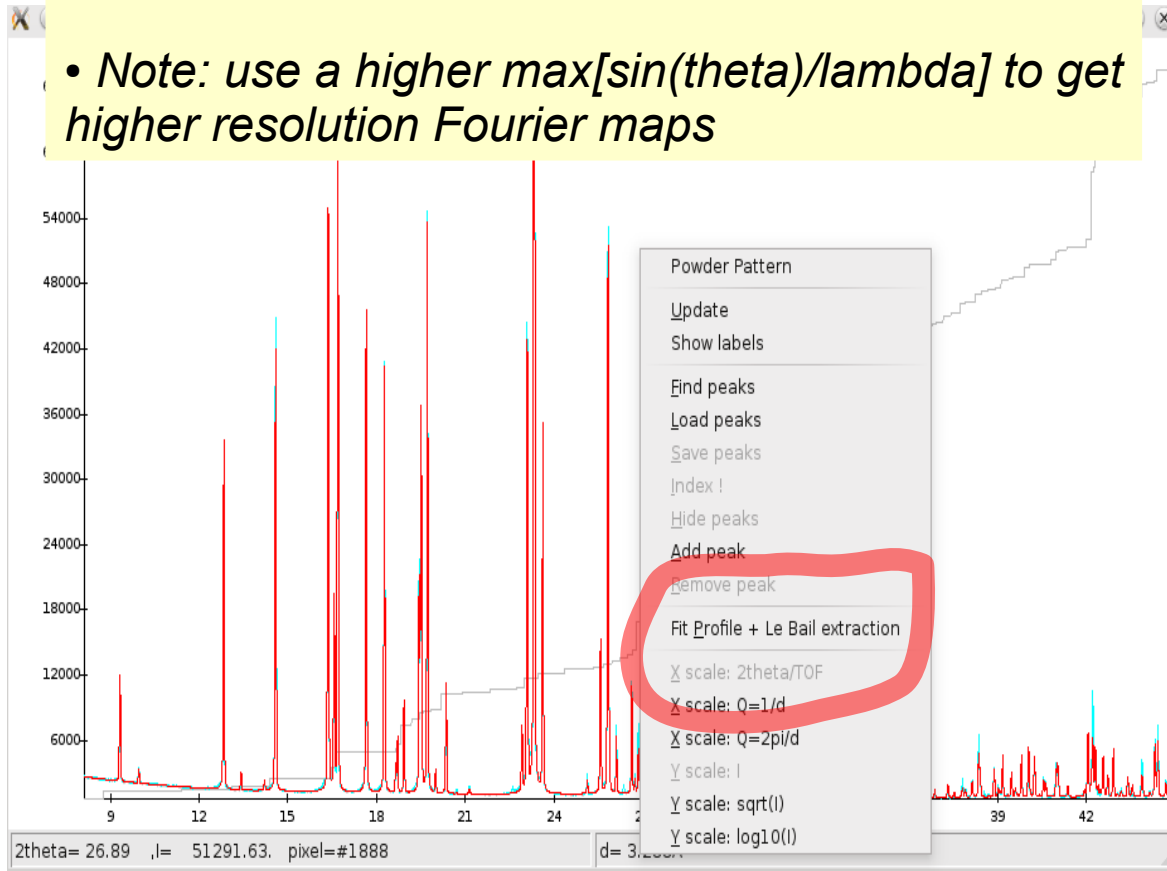
- Auto-indexing using the **dichotomy algorithm**
- Default search up to monoclinic
- Default search with **0-3 impurity lines**
- Search for **triclinic** (advanced tab, working since version 1.9)
- Automatic volume range selection
- Ability to select solution & perform profile fit

# Profile fitting & Le Bail extraction

- Fox is not too sensitive to exact profiles but it is still better to use fitted ones (for large overlaps)

- By default Fox refines parameters with increasing complexity (width -> symmetric profile -> asymmetric -> background -> cell...)

- Note: use a higher  $\max[\sin(\theta)/\lambda]$  to get higher resolution Fourier maps



The screenshot shows the 'Profile Fitting' software interface. It has three tabs: 'Quick Fit', 'Manual Fit', and 'Spacegroup Explorer'. The 'Manual Fit' tab is active, and a sub-tab 'Le Bail + Fit Profile!' is selected. A list of fit options is shown, all of which are checked:

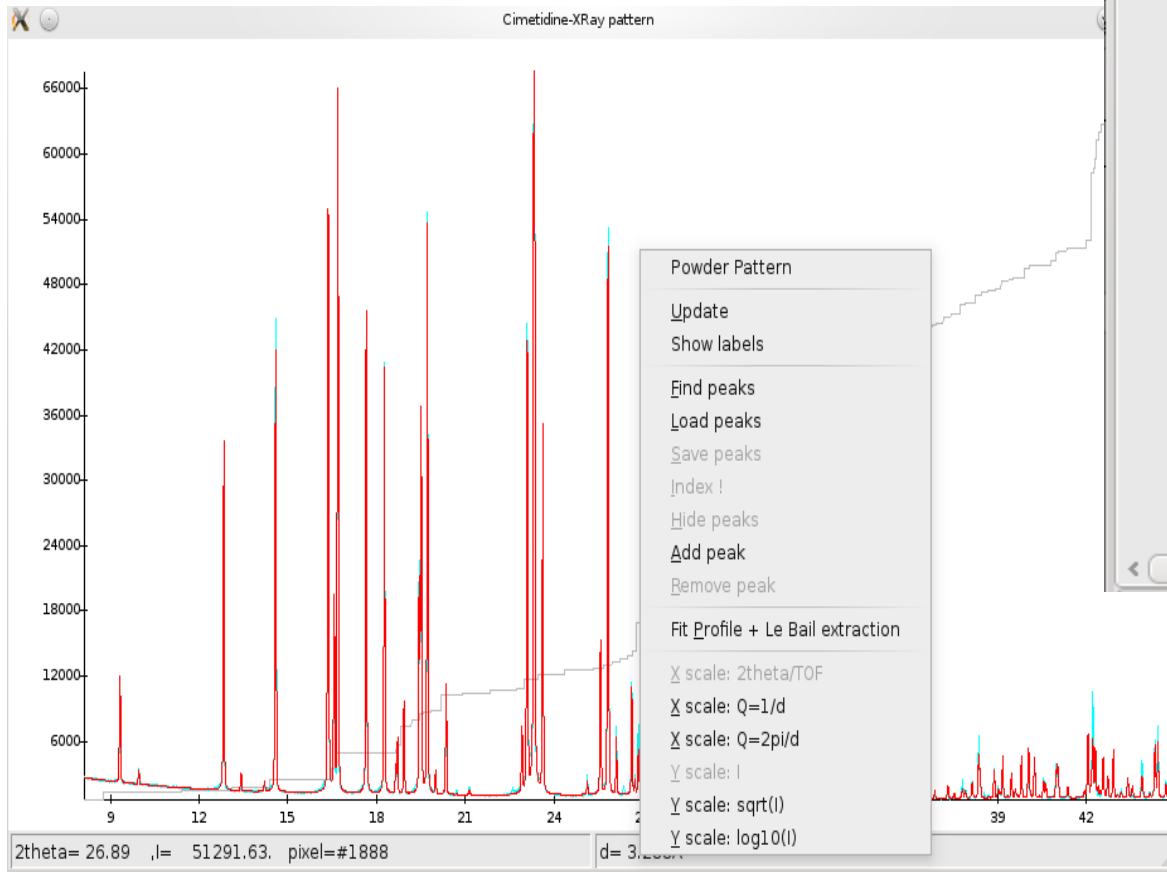
- Fit Zero shift
- Fit Constant Width
- Fit Variable Width
- Fit Gaussian-Lorentzian Mixing
- Fit Asymmetric parameters
- Fit Displacement+Transparency
- Fit Background
- Fit Unit Cell

Below the options, a log of fit cycles is displayed:

```
Starting 20 Le Bail cycles
=> Rwp=5.875%, GoF= 9.441
Fitting zero shift && constant width
=> Rwp= 5.872%, GoF= 9.433
Fitting width and gaussian/lorentzian fixed mix
=> Rwp= 5.866%, GoF= 9.412
Fitting gaussian/lorentzian mix
=> Rwp= 5.847%, GoF= 9.352
Fitting assymetry and sample displacement/transparency
=> Rwp= 5.842%, GoF= 9.336
Fitting background
=> Rwp= 5.821%, GoF= 9.270
Fitting unit cell
=> Rwp= 5.801%, GoF= 9.205
```

# Profile fitting & Le Bail extraction

- It is also possible to select individual parameters for a manual fit
- NB: enable tooltips and read them !

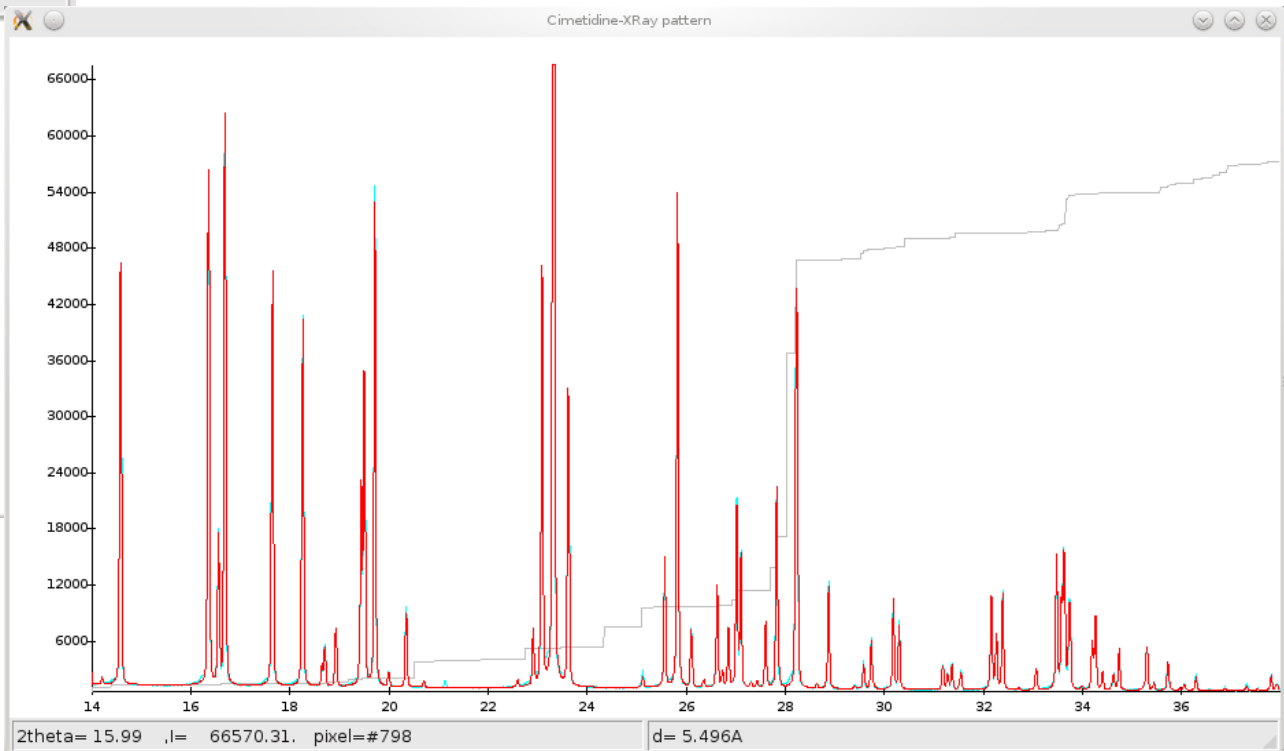
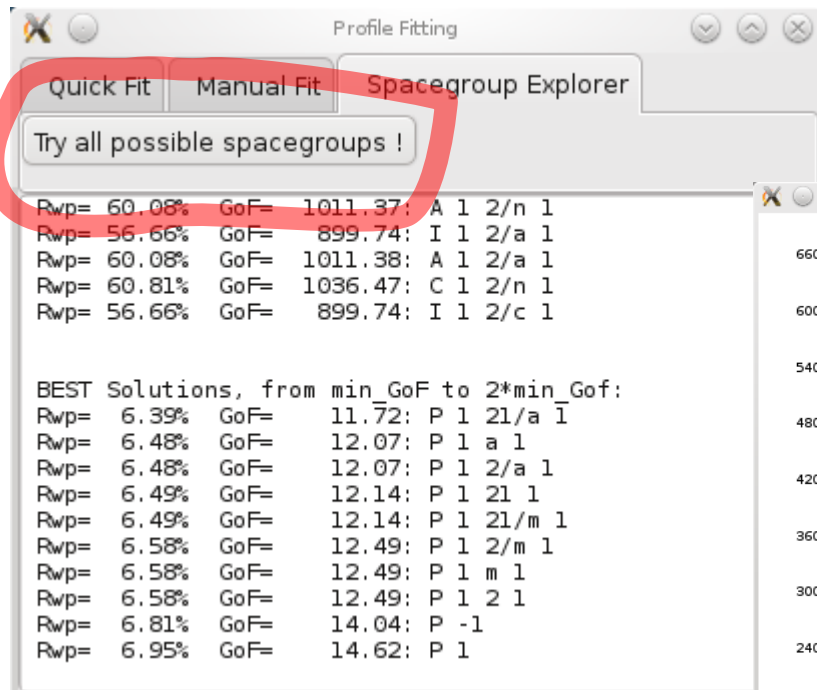


The 'Profile Fitting' dialog box is shown with the 'Manual Fit' tab selected. A red circle highlights the 'Manual Fit' tab. The dialog contains a list of parameters for fitting, each with a checkbox and a value. A tooltip is visible over the 'betaR' parameter, stating: 'Check this box to enable optimizing this parameter. (some parameters may be automatically fixed for global optimization)'. The parameters listed are:

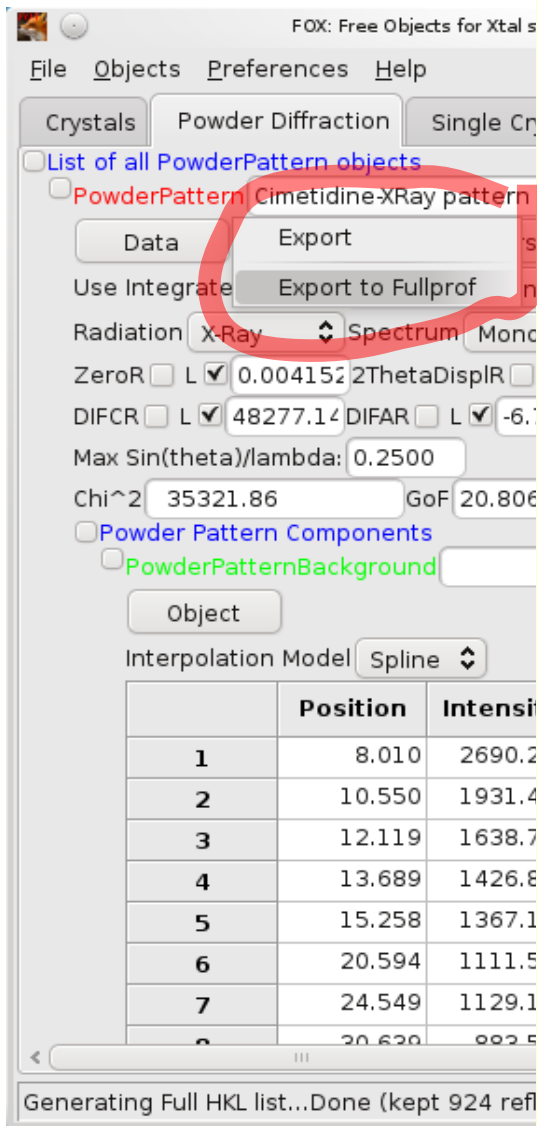
- name: [text box]
- aR  L  10.39420
- bR  L  18.81900
- cR  L  6.825030
- betaR  L  106.4369
- ZeroR  L  [text box]
- 2ThetaD  L  [text box]
- 2ThetaTranspR  L  0.001058
- DIFCR  L  48277.14
- DIFAR  L  -6.70000
- Scale\_R  L  0.000111
- WavelengthR  L  1.529040
- Background\_Point\_0R  L  2690.280
- Background\_Point\_1R  L  1931.469

# Profile fitting: spacegroup explorer

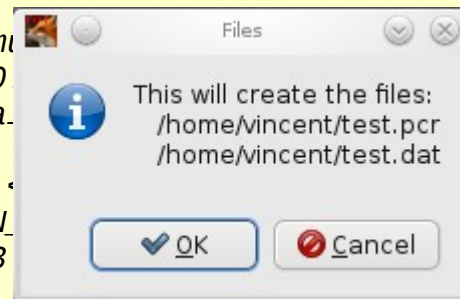
- Performs a profile fitting for all spacegroup settings allowed by the unit cell (37 for monoclinic cells, 478 for cubic cells... it can take a while).
- Spacegroups are listed by increasing GoF up to to  $2 * \min(\text{GoF})$



# Fullprof export



```
• 1 !Number of refined parameters
•! Zero Code Sycos Code Sysin Code Lambda Code More -> Patt #1
• 0.00415153 0.0 0.00119514 0.0 0.00105758 0.0 0.000 0.0 0
•!-----
--
•! Data for PHASE number: 0 ==> Current R_Bragg for Pattern# 1: 0.00
•!-----
--
•Cimetine
•!Nat Dis Ang Jbt Isy Str Furth ATZ Nvk More
•17 17 20 0 0 0 0 1.0 0 1
•!Jvi Jdi Hel Sol Mom Ter N_Domains
• 0 3 0 0 0 0 0
•!Contributions (0/1) of this phase to the patterns
• 1
•!Irf Npr Jtyp Nsp_Ref Ph_Shift for Pattern#0
• 0 0 0 0 0
•! Pr1 Pr2 Pr3 Brind. Rm
• 1.0 1.0 1.0 1.0 0
•! Max_dst(dist) (angles) Bond-Va
• 2.7000 1.5000 0
•P 1 21/a 1
•!Atom Typ X Y Z Biso Occ In Fin N
•C1 C 0.566876 0.342198 0.343369 3
• 0 0 0 0 0
•N2 N 0.448664 0.371933 0.388352 3 1 0 0 0 0
• 0 0 0 0 0
•C3 C 0.454253 0.405903 0.550729 3 1 0 0 0 0
• 0 0 0 0 0
•N4 N 0.586007 0.407123 0.696493 3 1 0 0 0 0
• 0 0 0 0 0
•C5 C 0.624978 0.44932 0.859614 3 1 0 0 0 0
• 0 0 0 0 0
•N6 N 0.663486 0.486503 1.01791 3 1 0 0 0 0
• 0 0 0 0 0
•N7 N 0.367983 0.448348 0.627608 3 1 0 0 0 0
• 0 0 0 0 0
•C8 C 0.222010 0.464022 0.452222 3 1 0 0 0 0
```



Pattern#0



# Fullprof export

FOX: Free Objects for Xtal

File Objects Preferences Help

Crystals Powder Diffraction Single Cr

List of all PowderPattern objects

PowderPattern Cimetidine-XRay pattern

Data Export

Use Integrate Export to Fullprof

Radiation X-Ray Spectrum Monochromator

ZeroR  L  0.004152 2ThetaDispLR

DIFCR  L  48277.14 DIFAR  L  -6.1

Max Sin(theta)/lambda: 0.2500

Chi^2 35321.86 GoF 20.806

Powder Pattern Components

PowderPatternBackground

Object

Interpolation Model Spline

	Position	Intensity
1	8.010	2690.2
2	10.550	1931.4
3	12.119	1638.7
4	13.689	1426.8
5	15.258	1367.1
6	20.594	1111.5
7	24.549	1129.1
8	28.620	882.5

Generating Full HKL list...Done (kept 924 refl)

```

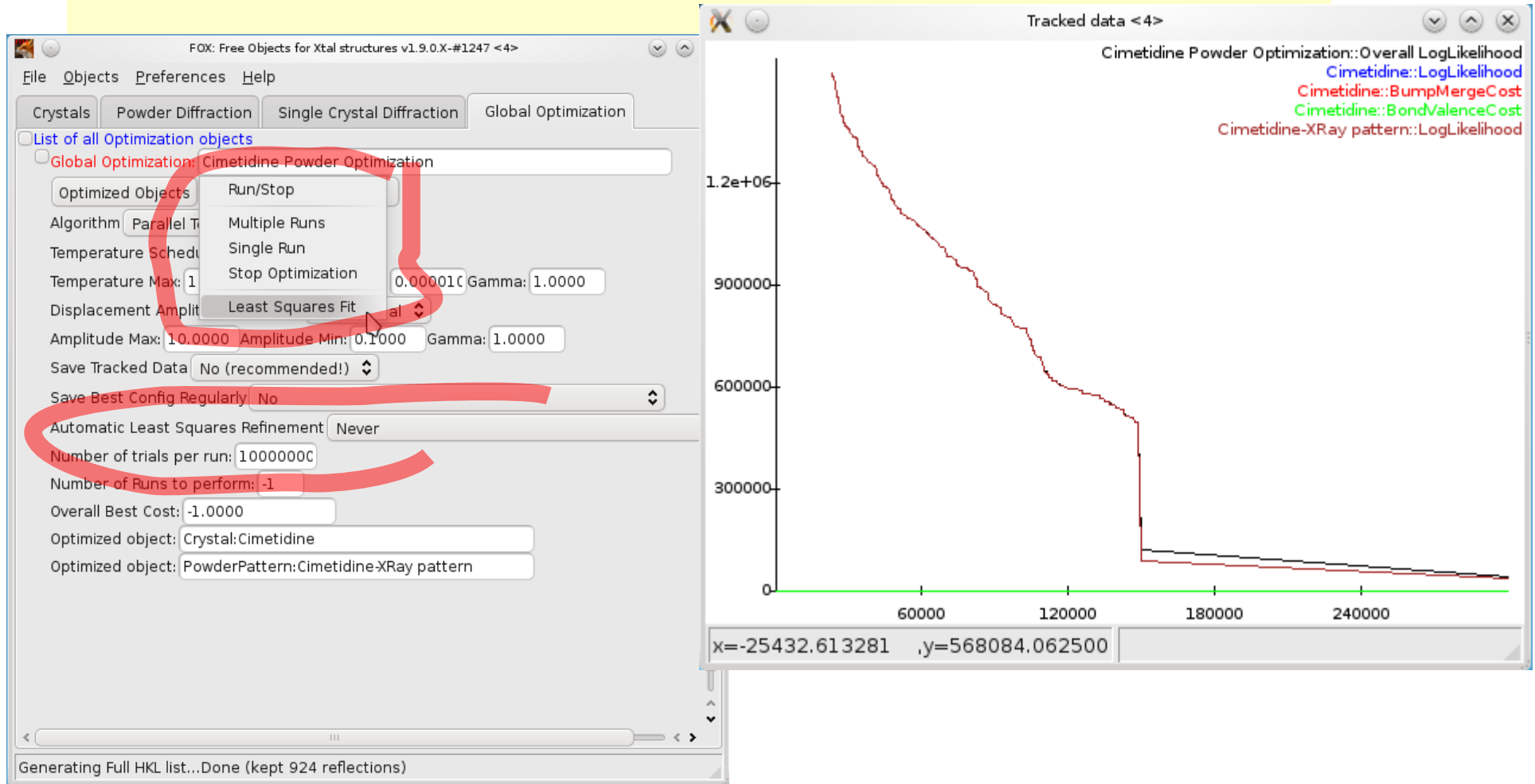
!      U      V      W      X      Y      GauSiz      LorSiz Size-Model
0.00341898 8.85951e-05 0.00156559 0.0 0.0 0.0 0.0 0.0
      0.0      0.0      0.0      0.0      0.0      0.0      0.0
!      a      b      c      alpha      beta      gamma      #Cel
Info
10.3942 18.819 6.82503 90 106.437 90
      0.0      0.0      0.0      0.0      0.0      0.0      0.0
! Pref1 Pref2 alpha0 beta0 alpha1 beta1 ?
      0.0 0.0 0.0 0.0 0.0 0.0
      0.0 0.0 0.0 0.0 0.0 0.0
!Soft distance constraints
C1 N2 1 0 0 0 1.47 0.01
N2 C3 1 0 0 0 1.4 0.01
C3 N4 1 0 0 0 1.4 0.01
N4 C5 1 0 0 0 1.37 0.01
C5 N6 1 0 0 0 1.13 0.01
C3 N7 1 0 0 0 1.4 0.01
N7 C8 1 0 0 0 1.47 0.01
C8 C9 1 0 0 0 1.54 0.01
C9 S10 1 0 0 0 1.82 0.01
S10 C11 1 0 0 0 1.82 0.01
C11 C12 1 0 0 0 1.5 0.01
C12 N13 1 0 0 0 1.37 0.01
N13 C14 1 0 0 0 1.37 0.01
C14 N15 1 0 0 0 1.37 0.01
N15 C16 1 0 0 0 1.37 0.01
C16 C17 1 0 0 0 1.5 0.01
C16 C12 1 0 0 0 1.45 0.01
!Soft angle constraints
C1 N2 C3 1 1 0 0 0 0 0 0 108.862 0.572958
N2 C3 N4 1 1 0 0 0 0 0 0 119.748 0.572958
C3 N4 C5 1 1 0 0 0 0 0 0 119.748 0.572958
N4 C5 N6 1 1 0 0 0 0 0 0 180 0.572958
N2 C3 N7 1 1 0 0 0 0 0 0 119.748 0.572958
N4 C3 N7 1 1 0 0 0 0 0 0 119.748 0.572958
C3 N7 C8 1 1 0 0 0 0 0 0 108.862 0.572958
N7 C8 C9 1 1 0 0 0 0 0 0 108.862 0.572958
C8 C9 S10 1 1 0 0 0 0 0 0 108.862 0.572958
C9 S10 C11 1 1 0 0 0 0 0 0 108.862 0.572958

```

# Least squares

Least squares refinement can be performed:

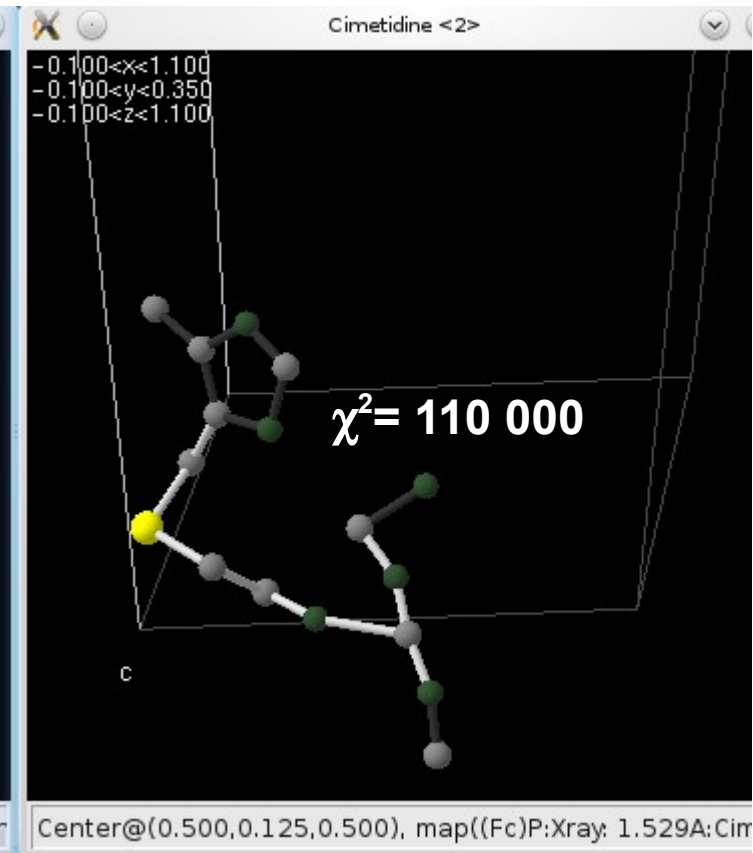
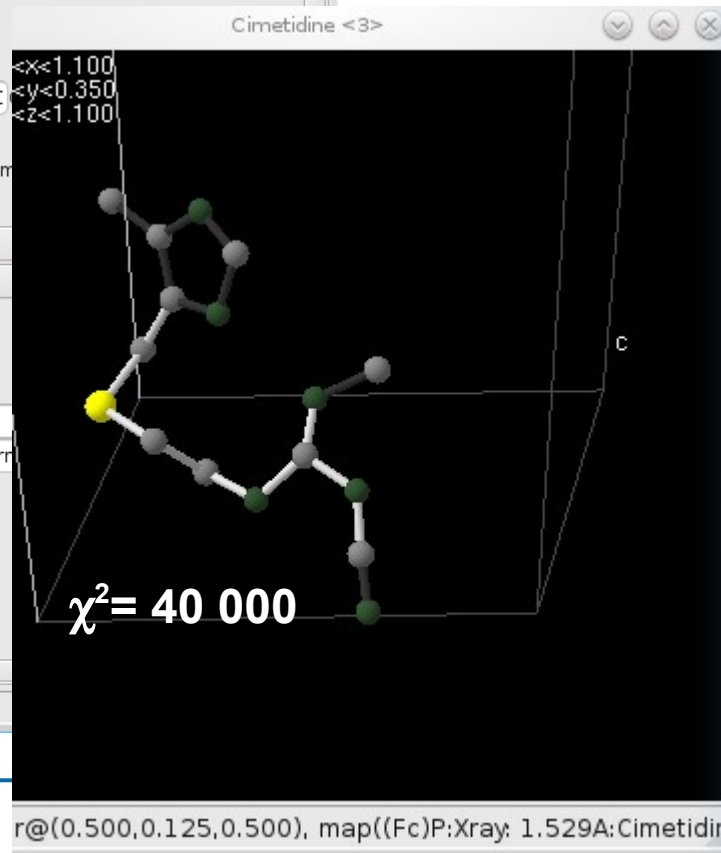
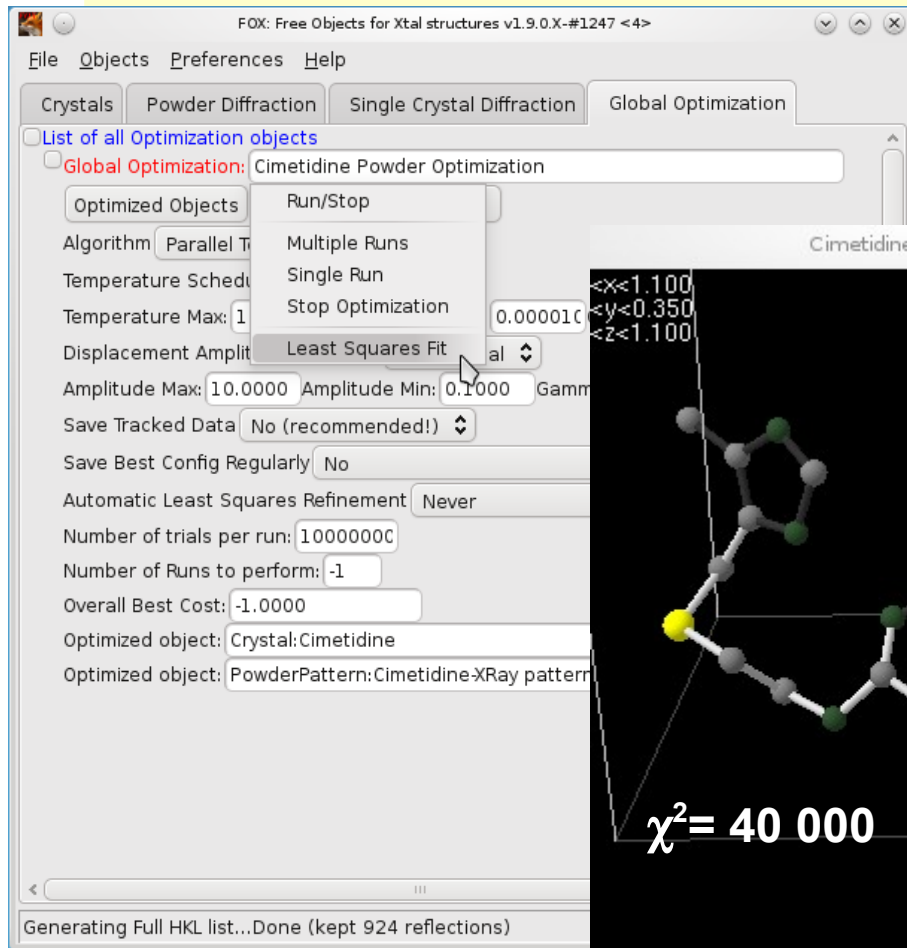
- For profile fitting
- After optimization (only the structure is refined, no parameter choice)
- **Automatically during global optimization**



# Least squares

Least squares refinement can be performed:

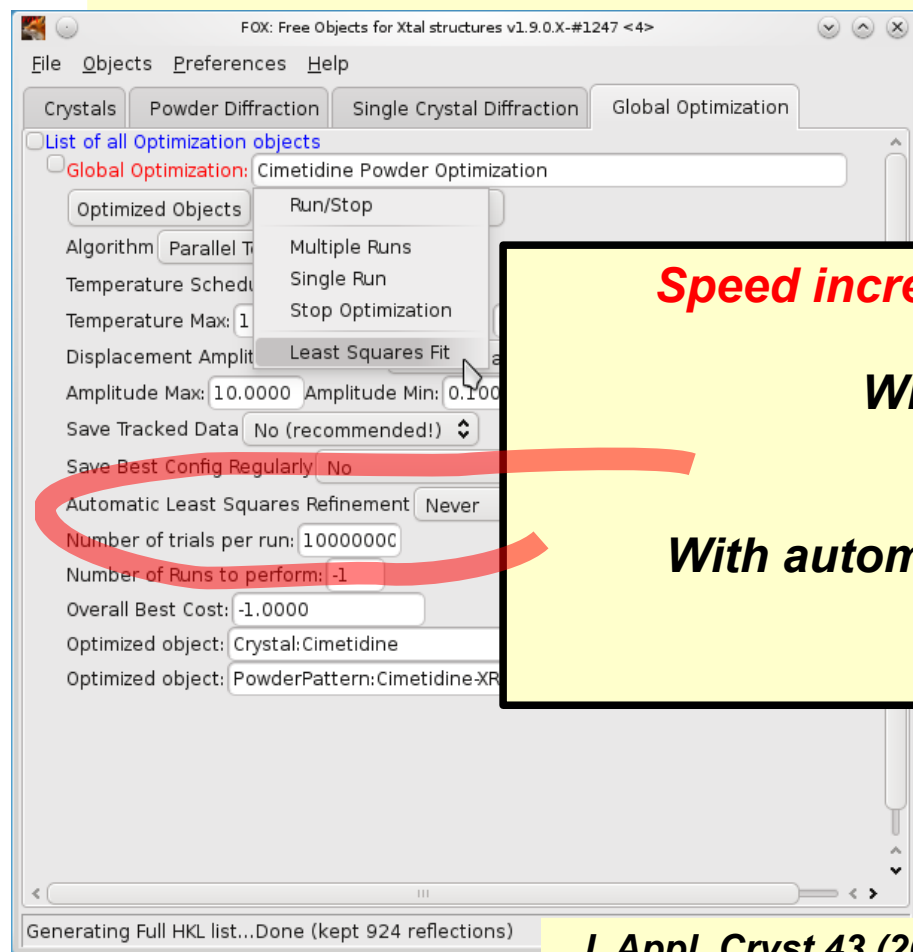
- For profile fitting
- After optimization (only the structure is refined, no parameter choice)
- **Automatically during optimization**



# Least squares

Least squares refinement can be performed:

- For profile fitting
- After optimization (only the structure is refined, no parameter choice)
- **Automatically during optimization**



**Speed increase for structure solution (Cimetidine) :**

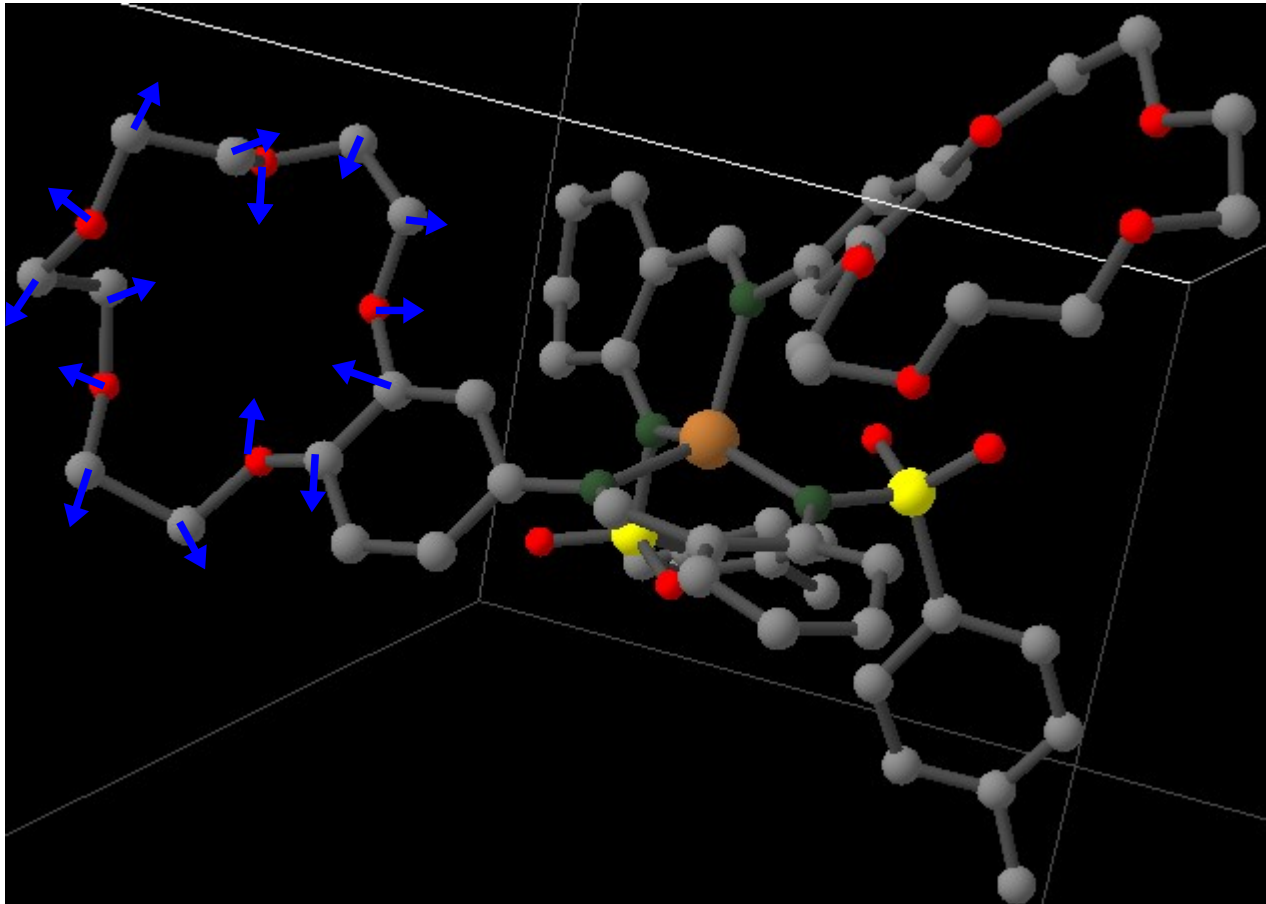
**Without automatic least-squares:  
 $1.6 \times 10^6$  trials**

**With automatic least-squares every 150 000 trials:  
 $6 \times 10^5$  trials (~2 minutes)**

**J. Appl. Cryst 43 (2010),401 : suggests global optimization can be performed by doing only downhill minimization from random starting points...**

# ***Model Building: Molecular Dynamics for Flexible Cycles***

# Using Molecular Dynamics

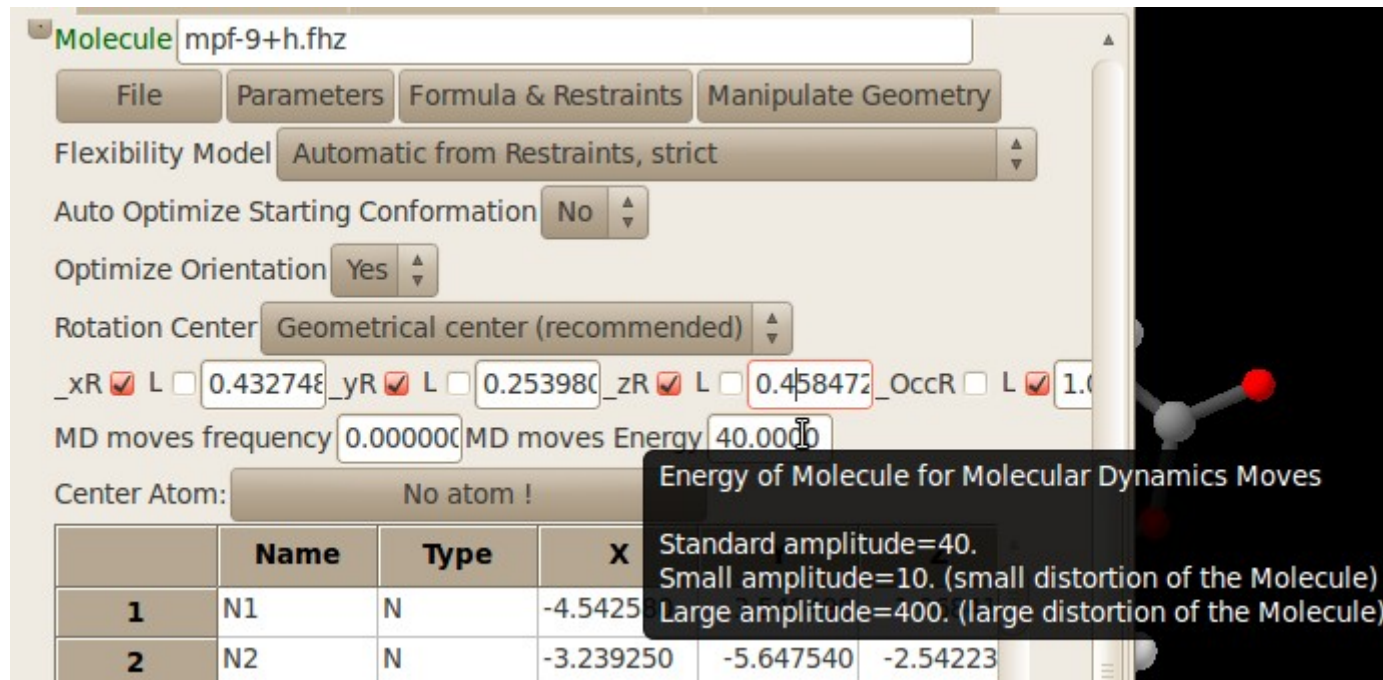


Atoms in “restrained” groups are moved using molecular dynamics principles :

- Each atom is given a random vector speed
- The overall Energy is  $E_{kinetic} + E_{restraints}$
- Atoms are moved according to standard mechanics (force=gradient of  $E_{restraints}$ )

•

# Using Molecular Dynamics



Molecule mpf-9+h.fhz

File Parameters Formula & Restraints Manipulate Geometry

Flexibility Model Automatic from Restraints, strict

Auto Optimize Starting Conformation No

Optimize Orientation Yes

Rotation Center Geometrical center (recommended)

\_xR  L  0.432748 \_yR  L  0.253980 \_zR  L  0.458472 OccR  L  1.0

MD moves frequency 0.00000 MD moves Energy 40.0000

Center Atom: No atom !

	Name	Type	X
1	N1	N	-4.5425
2	N2	N	-3.239250 -5.647540 -2.54223

Energy of Molecule for Molecular Dynamics Moves

Standard amplitude=40.  
Small amplitude=10. (small distortion of the Molecule)  
Large amplitude=400. (large distortion of the Molecule)

*MD moves are **computationally expensive***

*=> they are only tried once in a while*

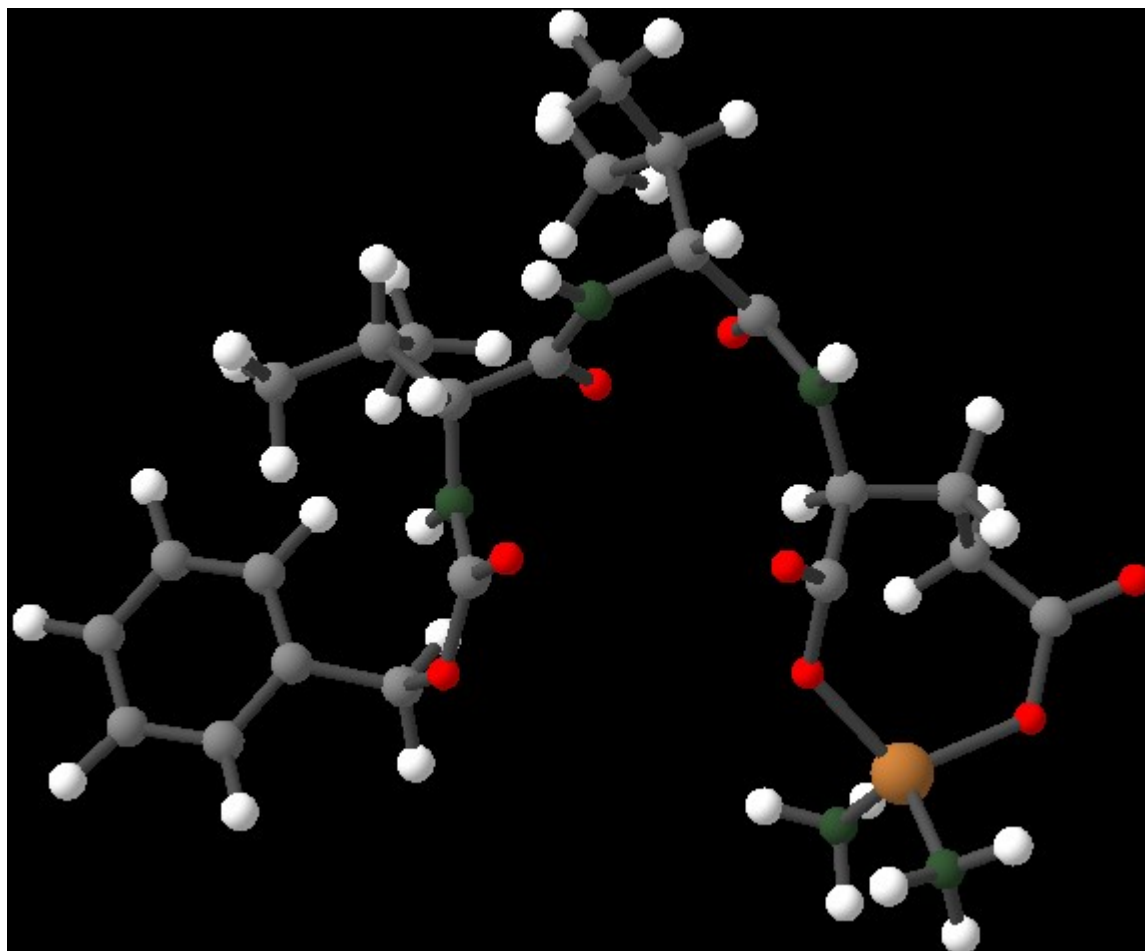
*=> the **frequency** can be chosen (by default: 0=never)*

*=> the **relative energy** of the molecule can be chosen to avoid too much distortion*

*... But remember that **SOME DISTORTION IS NECESSARY** to reach the 'true' conformation of the Molecule, starting from an incorrect one...*



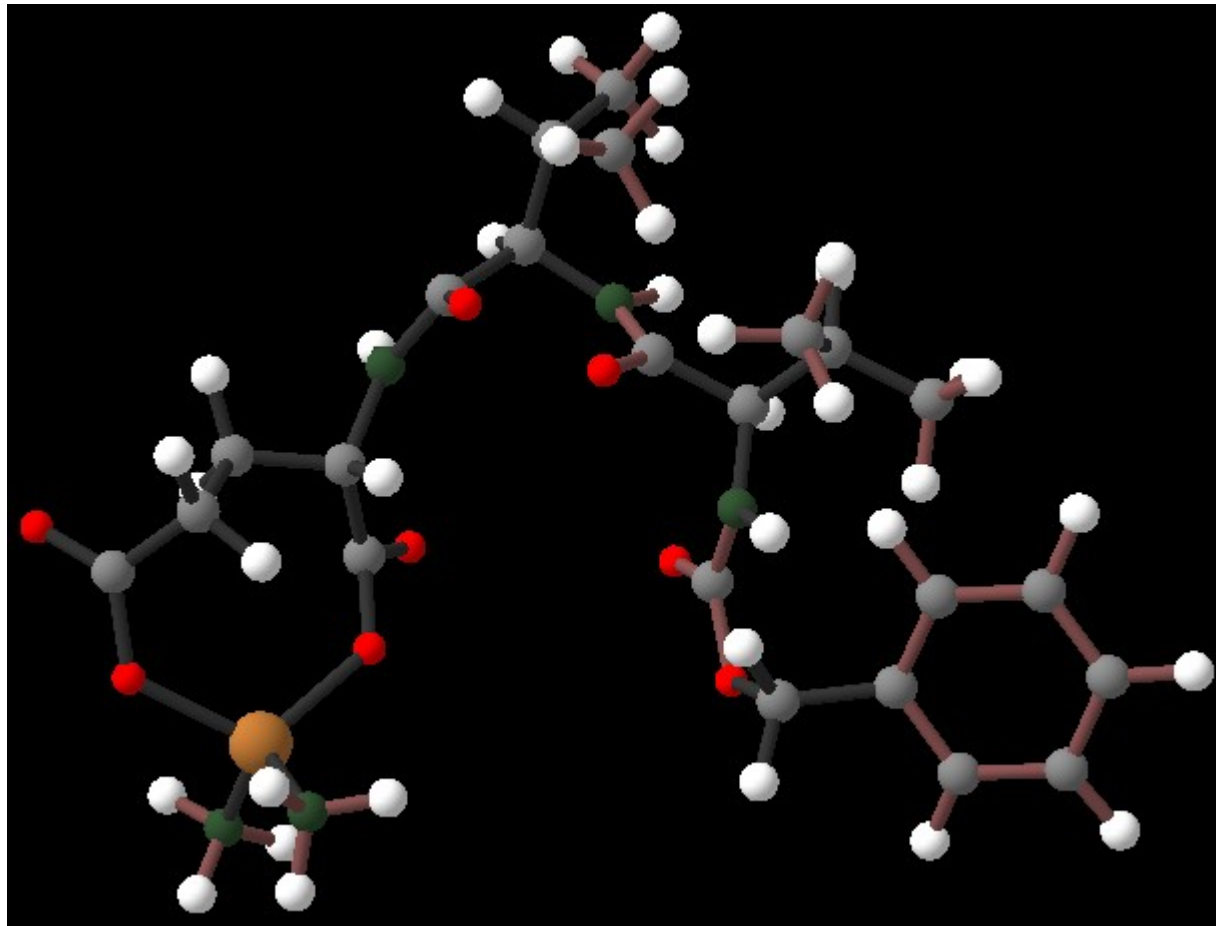
# Using Molecular Dynamics + least squares



***MD moves allow to solve complex, flexible structures with large cycles...  
...but it can take a long time !***

***Using **periodic least squares** greatly helps the convergence, as the least squares algorithm moves all the atoms individually (taking into account restraints) and is not limited by simple moves, or a z-matrix description***

# ***Molecular Dynamics + least squares + rigid bodies***



***SOME DISTORTION IS NECESSARY... but sometimes you really want to avoid it  
=> You can create 'rigid groups' of atoms that will only be translated/rotated as  
a rigid body, even during least squares.***

# Using Fox

From the wiki: <http://objcryst.sf.net>

<b>FOX</b>
Fox Home Page (wiki)
SourceForge Project
<b>About FOX</b>
Download
Install
Screenshots
Biblio: Fox References
Biblio: Structures solved
Mailing List
FAQ
<b>Using FOX</b>
Tutorials
FOX Manual (intro.)
- Crystal Structures
- Powder Diffr. data
- Single Crystal data
- Optimization Algo.
<b>FOX Development</b>
Current Development
Features Requests
ObjCryst++ API
Getting FOX from SVN
Browse Code Repository

**Download & Install**  
(Linux, MacOS X,  
Windows)

**Manual, Tutorials**

The screenshot displays the FOX software interface. The main window shows a 3D model of a PbSO4 tetrahedron with atoms represented by spheres (Pb in grey, S in yellow, O in red). A red text box labeled "Graphical Interface" is overlaid on the model. Below the model is a powder diffraction pattern with peaks labeled with Miller indices (hkl). The interface includes a menu bar (File, Objects, Window, Help) and a toolbar. The bottom panel shows optimization data for various models, including PbSO4-joint, PbSO4-Tetrahedron, and PbSO4-XRay, with a plot of LogLikelihood vs. iteration number.

**command-line usage:**

```
Fox example/pbso4-joint.xml --nogui --randomize -n 100000 --nbrun 10  
--finalcost 1000 -o test.xml
```

# Outlook & Acknowledgements

**After 10 years... Fox can now index, fit profiles, ... and still solve structures !**

## **Projects:**

- **Update tutorials**
- **(much faster) least squares refinements**
- **Efficient protein flexibility**
- **More tests for Fox.Grid**
- **Inter-atomic restraints (complicated) ?**
- **FoxFlip (charge flipping) ??**
- **Contribute to pyobjcryst**



## **Thanks to:**

- **Radovan Cerny (U. Geneva)**
- **Jan Rohlíček, Michal Hušák (ICT Prague)**
- **Mark Pitt (TOF), Anders Markvardsen (help with Max Likelihood)**
- **Brian Toby + Michael Polyakov (Fourier maps display)**
  
- **Lachlan Cranswick... for too many reasons to list...**

**Improvements depend on **user feedback** !!! Send feedback, feature requests !**

**open-source** project => add your contribution

=> help by testing "development" versions (subscribe to the **mailing list!**)

=> send **bug reports** (also for cif import in openbabel)

**Get FOX from <http://objcryst.sourceforge.net>**